



Primordial Elements: Double Trouble

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Checkpoints

- Abundance basics
- Big Bang Nucleosynthesis (BBN) Overview
- Primordial Element Problem(s)
 - Lithium Problem
 - Deuterium Problem?



Abundances 101

- Ratio of some element to another (usually H)
- Notations/Representations

– Mass fraction $X_i = \frac{\rho_i}{\rho_{tot}}$

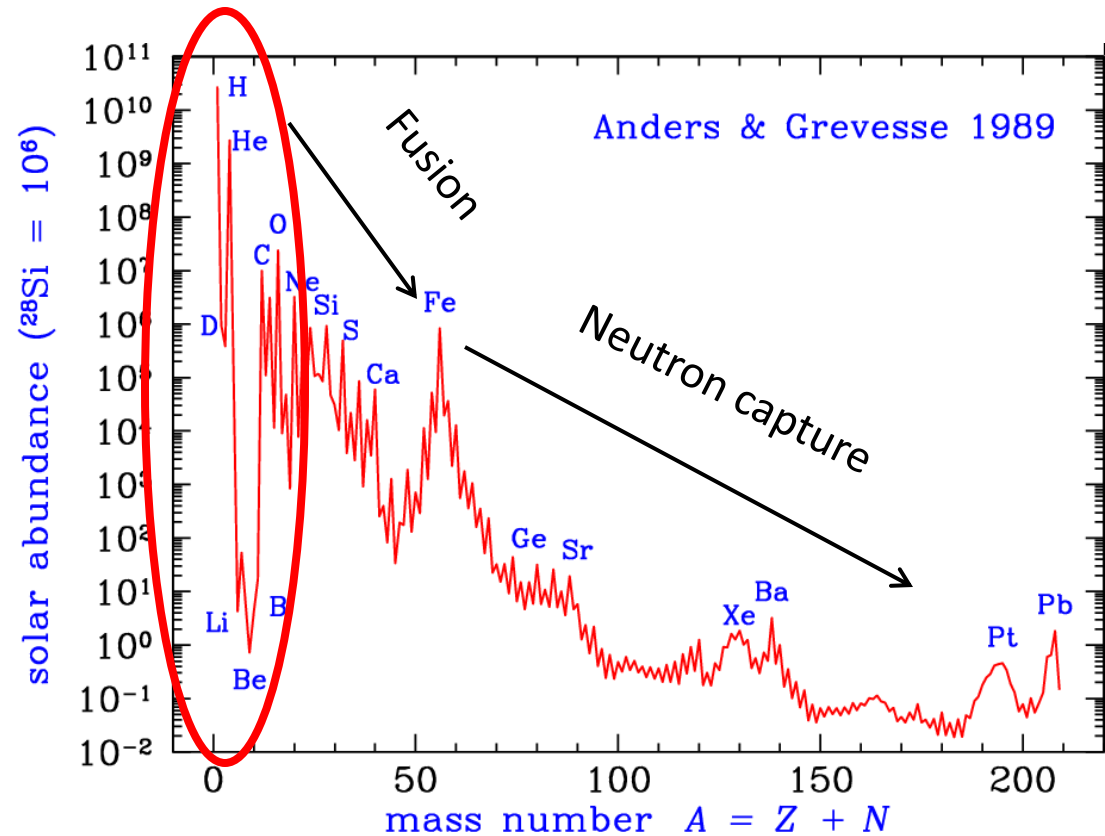
$$X \equiv X_H \quad Y \equiv X_{He} \quad Z \equiv X_{metal}$$

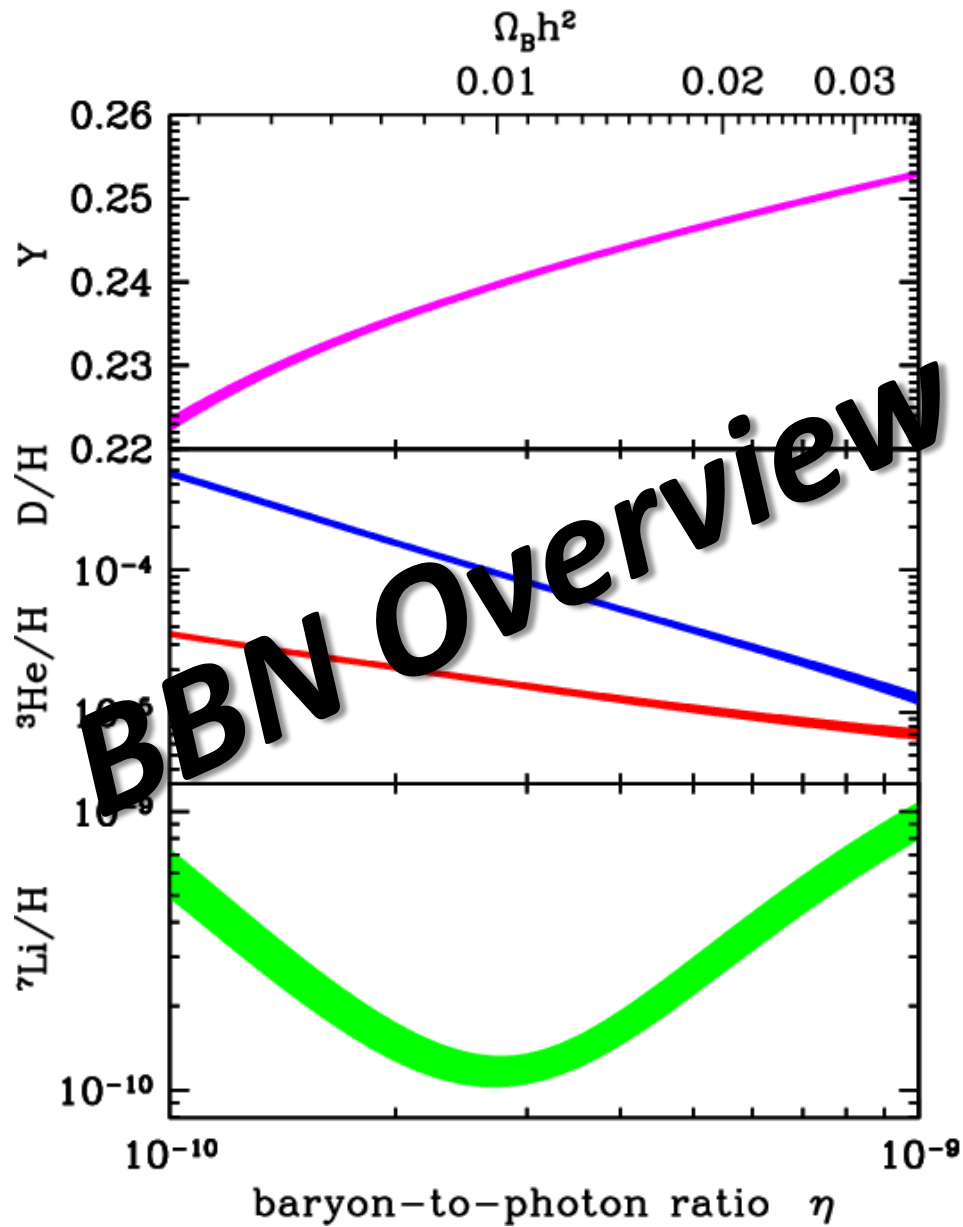
– Abundance (wrt H, by number) $\frac{i}{H} \equiv y_i \equiv \frac{n_i}{n_H}$

$$y_{He,sol} = 0.1 \quad y_{Fe,sol} \equiv \left(\frac{Fe}{H} \right)_{sol} = 3.2 \times 10^{-5}$$

Start: Solar Abundances

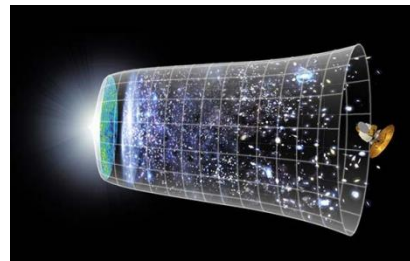
- Drop towards high mass numbers
 - Increasing Coulomb barrier
- Zig-zag pattern
 - Odd vs even
- LiBeB drop
 - Inefficient LiBeB fusing in BBN
- Iron peak - equilibrium
- $A \sim 130, 200$ peaks - s (low) & r (rapid) processes (neutron capture)





Three Pillars of Cosmology

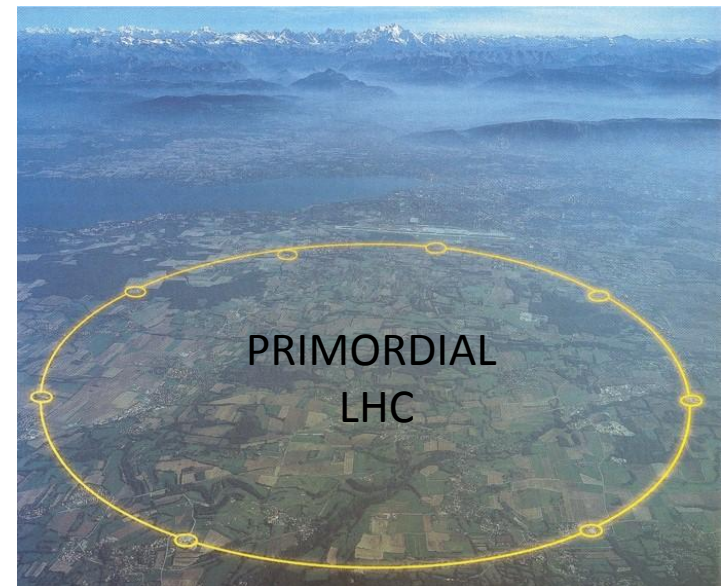
Observational evidence of the Big Bang Model



- I. Hubble Expansion $\sim T+10^{10}$ yr
- II. Cosmic Microwave Background $\sim T+4 \times 10^5$ yr
- III. **Big Bang Nucleosynthesis (BBN)** $\sim T+1$ sec.
The earliest probe!

Primordial Nuclear Reactor

- Hot, dense, expanding Universe
 - Synthesis of lightest elements – D, ^3He , ^4He , ^7Li
 - Race against expansion (faster expansion-less time for BBN!)
- Initial conditions + physics
- Get primordial abundances
- Compare with observations
- Test physics and cosmology!



Standard BBN: Framework

- Standard model of particle physics + Λ CDM cosmology
- General relativity
- Expanding, homogeneous Universe

– Friedmann equation $\left(\frac{\dot{a}}{a}\right)^2 \equiv H^2 = \frac{8\pi}{3} G\rho$

$a(t) = \frac{1}{1+z}$ Cosmic scale factor

$\rho = \sum_i \rho_i$ Mass energy density of all cosmic species

The Key

- Only one free parameter! Controls SBBN!

Baryon-to-photon ratio

$$\eta \equiv \frac{n_b}{n_\gamma} = 2.74 \times 10^{-8} \Omega_b h^2$$

$$\Omega_b = \frac{\rho_b}{\rho_{crit}} \quad \rho_{crit} = \frac{3H_0^2}{8\pi G}$$

- Constant! BBN determines baryon density!

$$\left. \begin{array}{l} n_\gamma \propto T^3 \\ n_b \propto a^{-3} \propto T^3 \end{array} \right\} \Rightarrow \eta = \text{const.} \sim 10^{-9}$$

Initial Conditions

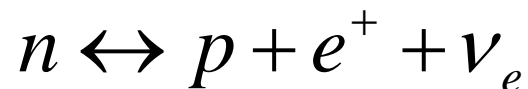
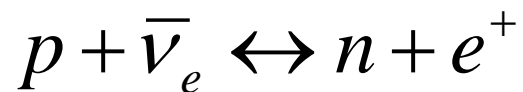
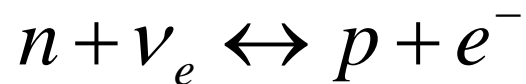
- $T \sim 1 \text{ MeV}$, $t \sim 1 \text{ sec}$
- Cosmic radiation
 - Thermal photons and (anti)neutrinos - Relativistic ($m \ll T$)
 - Electrons and positrons – $m < T$
- Cosmic matter
 - Neutrons and protons – non-relativistic $m \gg T$
- Radiation-dominated epoch
 - Dynamics dictated by radiation species

$$\rho_{rad} \gg \rho_{mat}$$

Tijana Prodanovic @ SF Cosmology Workshop
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Just before...

- $T > 1 \text{ MeV}$, $t < 1 \text{ sec}$
- Nucleons in equilibrium
 - Fast ($\Gamma_{n \leftrightarrow p} \gg H$) weak interactions



Weak Freeze-out

- Expanding, cooling universe favours lighter protons
- At $T \sim 0.8 \text{ MeV}$, $t \sim 1 \text{ sec}$.
- Reaction rates not fast enough for expansion

$$\Gamma_{n \leftrightarrow p} \ll H$$

- Nucleon conversion reactions stop

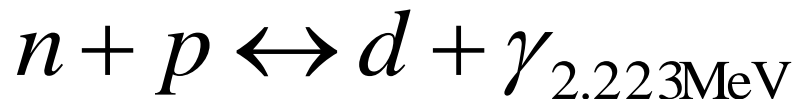
- Ratio freezes @ $\frac{n}{p} \approx \frac{1}{6}$

$$\frac{n}{p} = e^{-(m_n - m_p)/T}$$



Deuterium Bottleneck

- Must form D before fusion can proceed



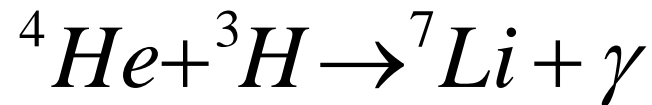
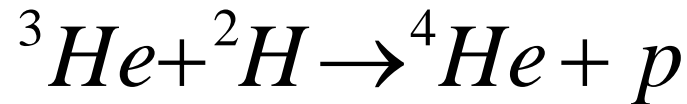
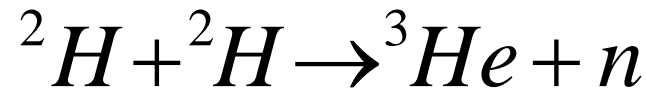
- But! 2.2 MeV photons destroy D!
- Most photons have $T < 1$ MeV but still enough of 2.2 MeV photons in thermal tail
- Must wait for deuterium!
- Neutrons keep decaying (~ 10 min)



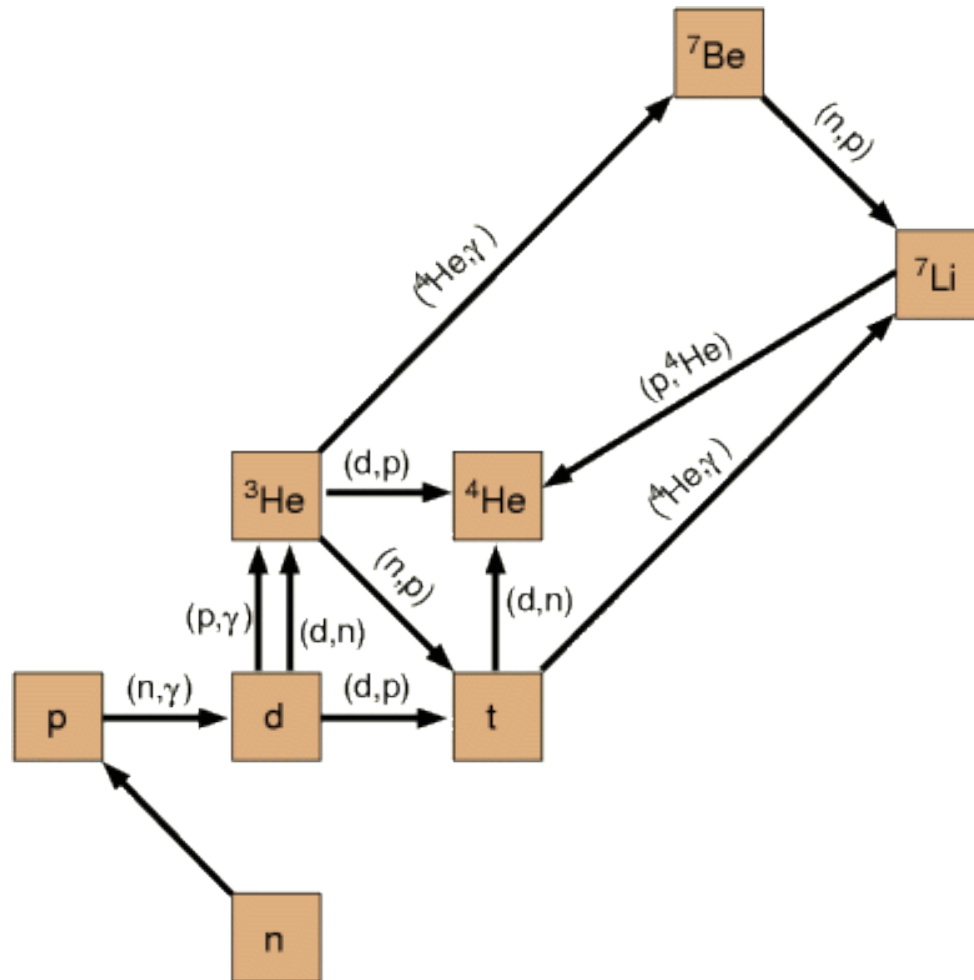
$$\frac{n}{p} \rightarrow \frac{1}{7}$$

Fusion time!

- At $t \sim 3$ min, $T \sim 0.07$ MeV
- D abundance rises fast!
- Light elements are fused! Main reactions:



BBN Reactions Network



The Outcome

- ${}^4\text{He}$ very stable – production favored
- No stable nuclei at $A=5$ and $A=8$ - heavier element production suppressed
 - For heavier, must fuse D, T or ${}^3\text{He}$ with ${}^4\text{He}$
 - Large Coulomb barrier
- Most neutrons go into ${}^4\text{He}$
 - He not very sensitive to baryon density

$$Y_p \cong 0.24$$

The Outcome

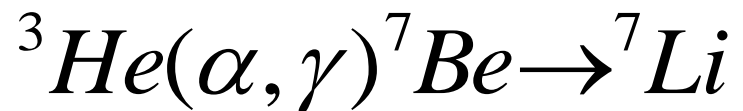
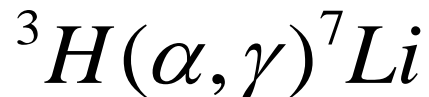
- Incomplete nuke burning
 - Not all neutrons used up
 - Traces of D, ^3He and ^7Li
 - Trace abundance strongly dependant on nuke freezeout T - baryon density
- BBN stops @ $T \sim 30 \text{ keV}$, $t \sim 20 \text{ min}$

Nuclear freezeout!

(except for the unstable ones – remaining ^3H decays,
 $^7\text{Be} + e \rightarrow ^7\text{Li}$)

Primordial abundances vs. Baryon-to-photon ratio

- If higher nucleon (baryon) density
 - BBN starts earlier – more nucleons, higher temp., more complete burning
 - More ^4He made
 - Less D and ^3He left
 - Li made 2 ways:



Less stable under proton collisions

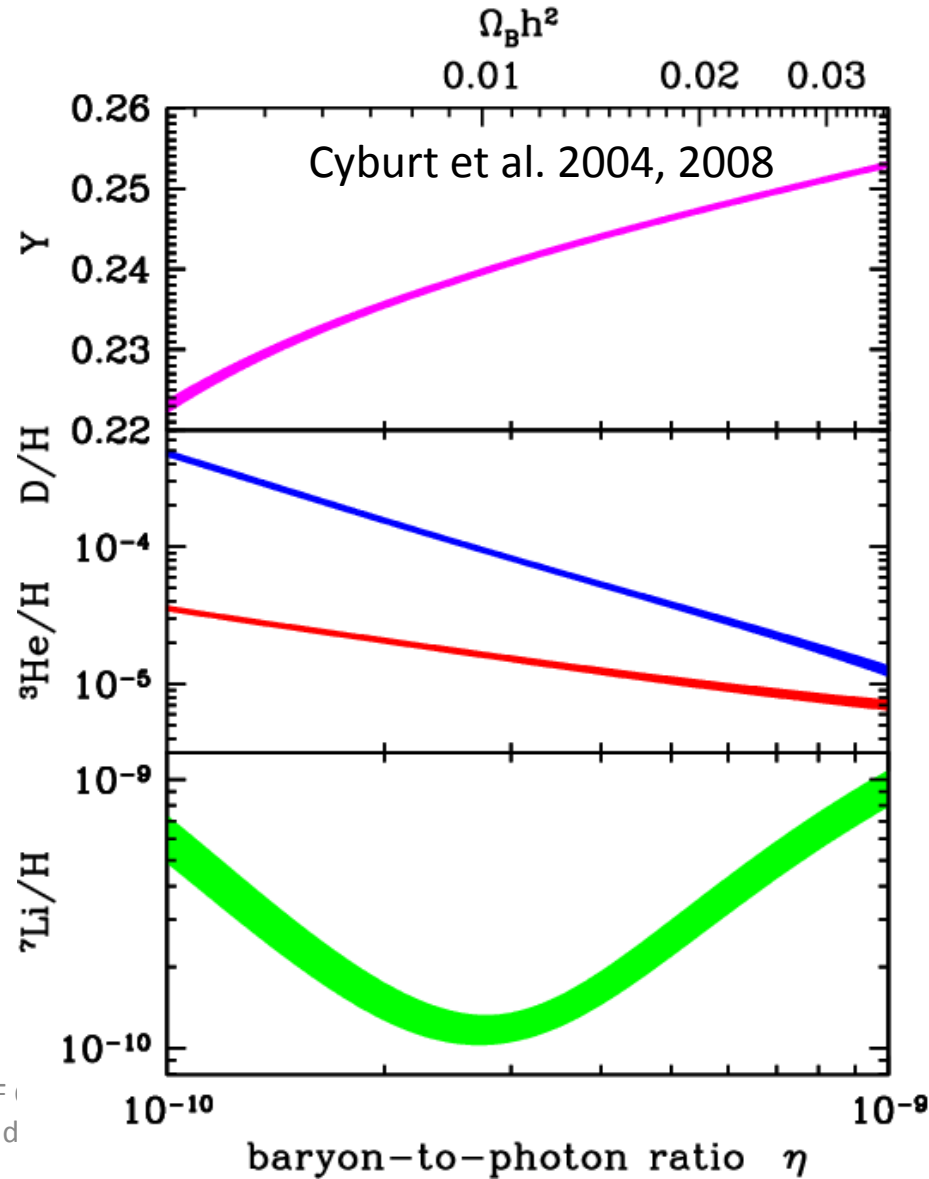
Strongly bound

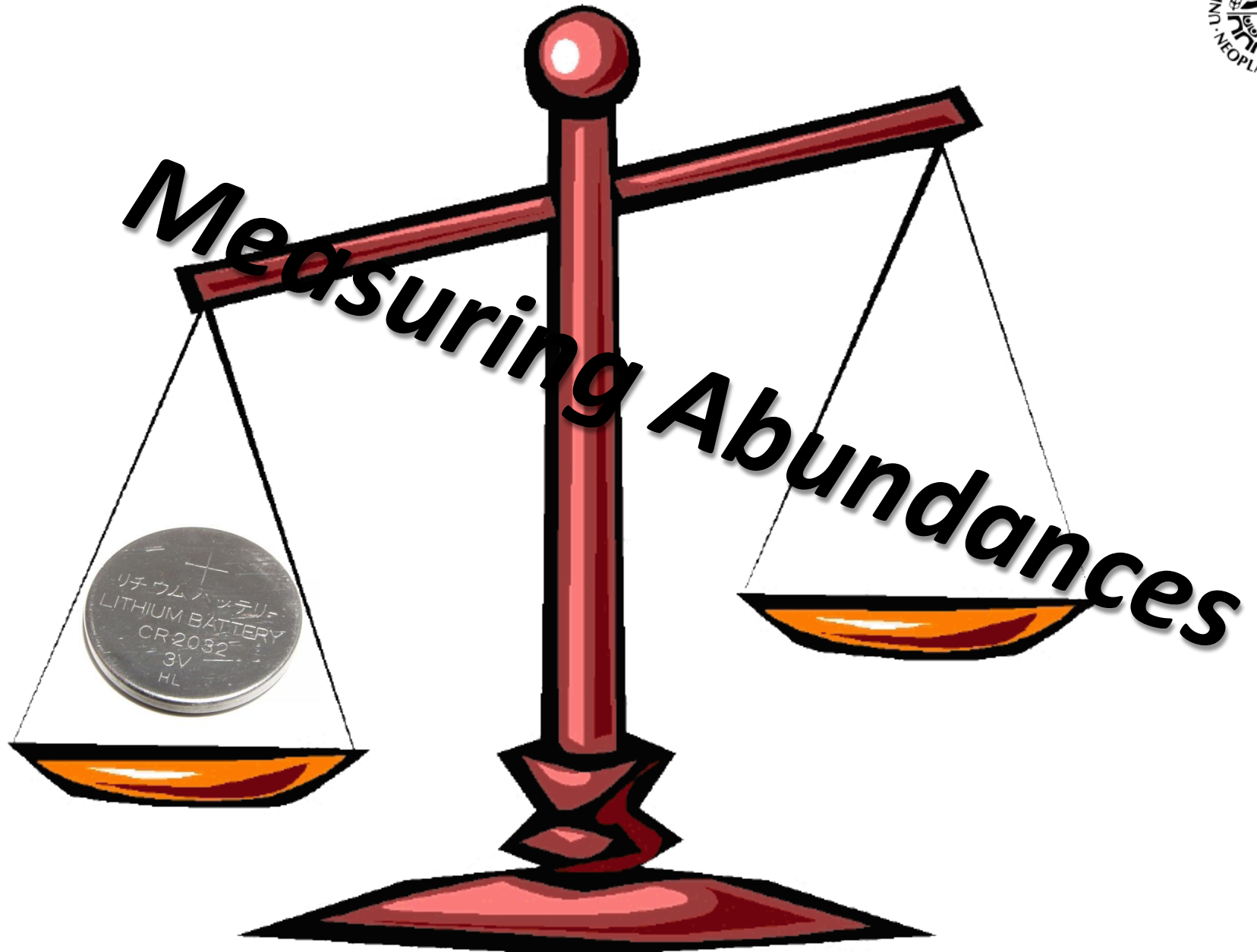
Dominates at low baryon-to-photon Dominates at high baryon-to-photon



SBBN Predicted Abundances

- Schramm plot
- Abundance vs. Baryon density
- Curves: SBBN
- 1σ errors – nuclear cross-sections
- Measure abundance!
- Done!





Stuck in the future

- Abundances today not same as after BBN
- Look at (close) to primordial systems – low metallicity
 - Correct for $t_{BBN} \neq t_{obs}$ changes as best as you can
- Where to look?
 - D – absorption towards QSO (UV)
 - ^3He (II) – emission in galactic HII regions
 - ^4He (II, III) - emission in extragalactic HII regions
 - ^7Li – absorption in atmospheres of low-metallicity halo stars
- Different systems but look for concordance?

Hopeless ^3He ...

- Complicated history
 - Stars burn D to make ^3He , burned to make ^4He
 - More survives in cooler stars
 - Net production...but depends on destruction-production balance
- Only observed in Galactic HII regions – hyperfine transition
- Must extrapolate from today to BBN epoch
- Too model dependant!

Hopefull ^4He

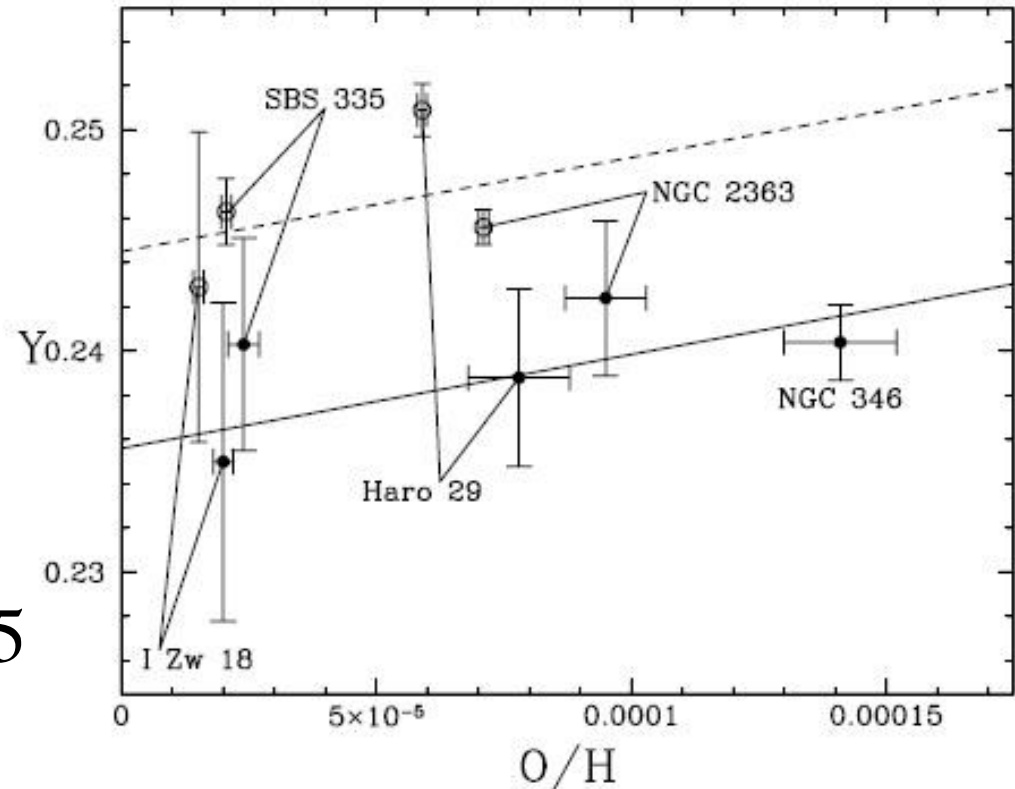
- Produced in stars
- Stable – once create, difficult to destroy
- Net increase with time
- Back in time – primordial plateau should exist
- Measured in low-metallicity extragalactic HII regions
- But note... "spherical cow"



Hopefull ^4He

- ^4He vs. Metallicity (oxygen)
- Extrapolate to 0 metal.

$$Y_{p,obs} = 0.2384 \pm 0.0025$$



Peimbert et al. 2002

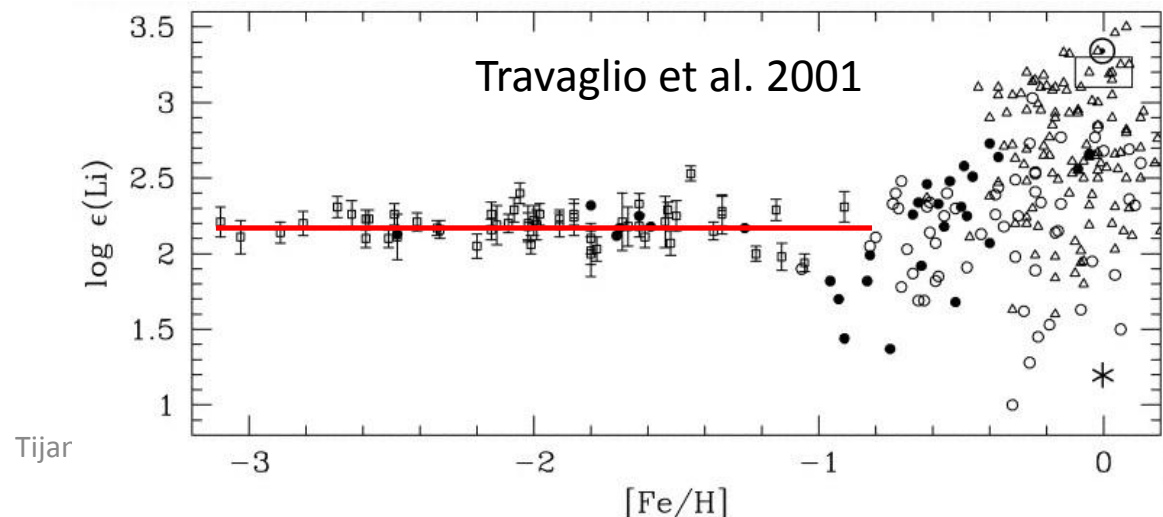
Promissing ${}^7\text{Li}$

- Fragile, destroyed in stars
- But produced in CR interactions (fusion, spallation) and neutrino-process in SN
- At low metallicity should see a plateau
- Pop II, low-metallicity, cold halo stars

- **Spite plateau**

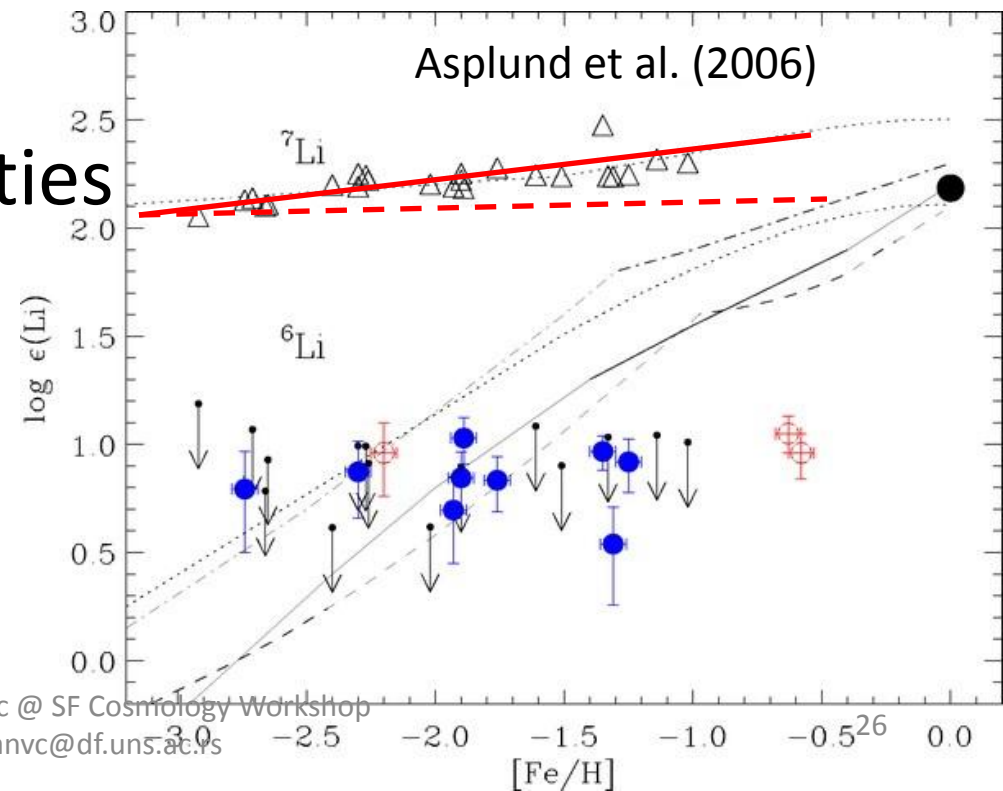
Spite & Spite (1982)

- **Primordial Li!**



Promising ${}^7\text{Li}$

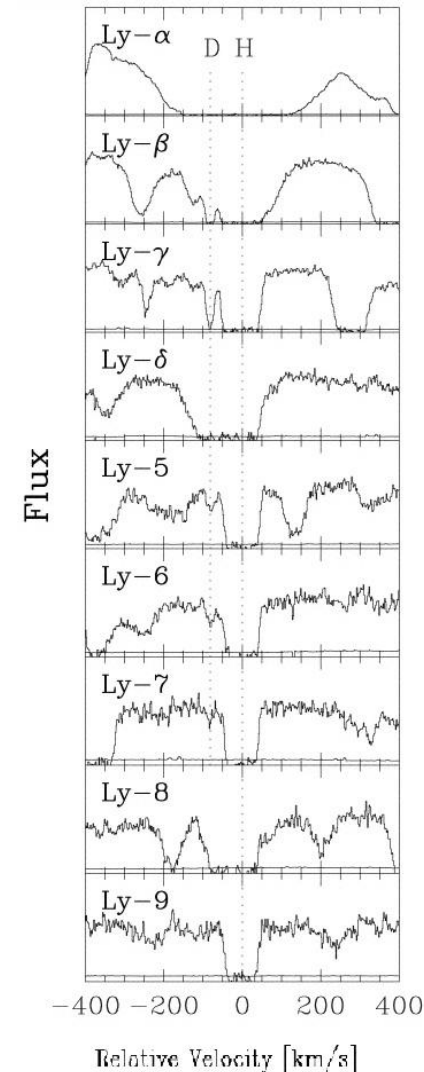
- Spite plateau?
- More data reveal a slope
- Pre-galactic Li (rather than primordial)
- Stellar modeling – systematic uncertainties
 - Temperature scale
 - Mixing (Li fragile!)



Deuterium - Baryometer of Choice

- Strong baryon density dependance
- Very fragile – simple history
- Only net destruction (Epstein et al. 1976, Prodanovic & Fields 2003) – stellar processing
- Easy to extrapolate to zero metallicity
- Observe in high-z quasar absorption Ly α systems
 - Quasars @ $z \sim 3$ in the background of a cold H cloud
 - D not same as H! Line shifted!

O'Meara et al. 2001
 QSO: HS 0105+1619



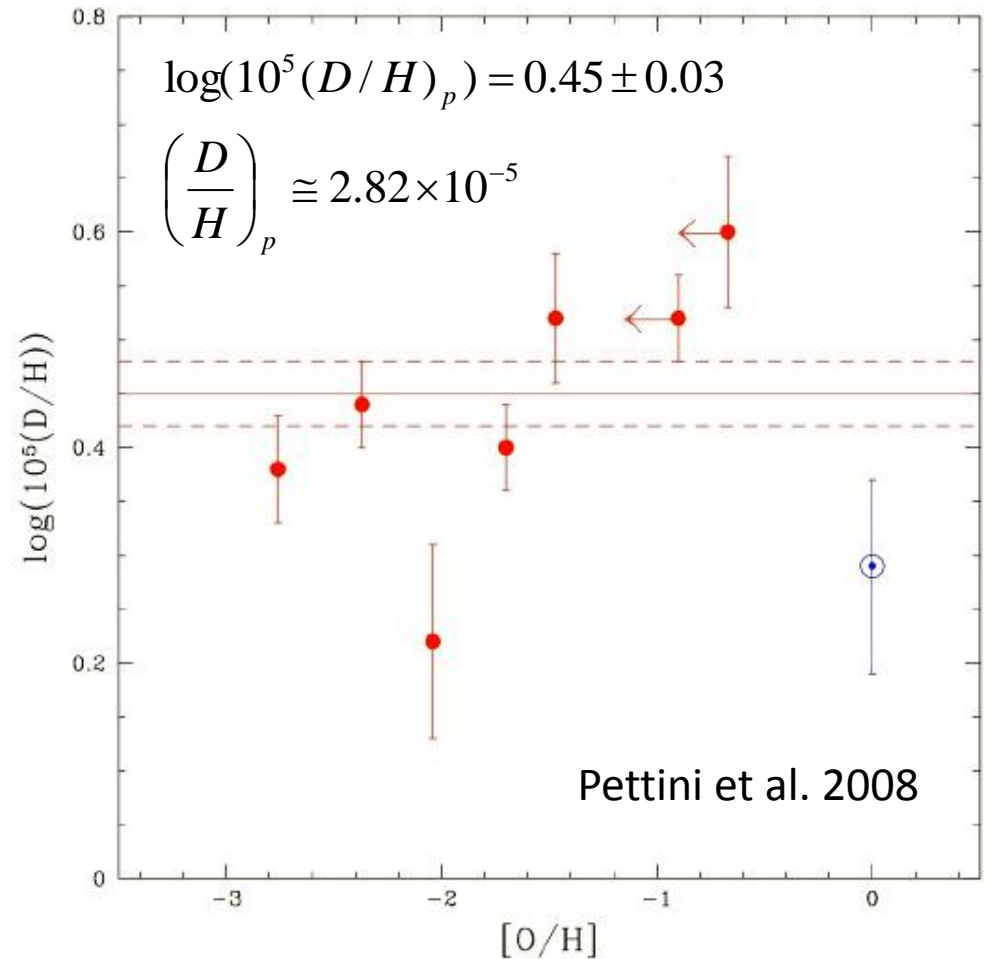
Deuterium - Baryometer of Choice

- Evolution of D with metals

$$D \sim e^{-Z/Z_{sol}} D_p$$

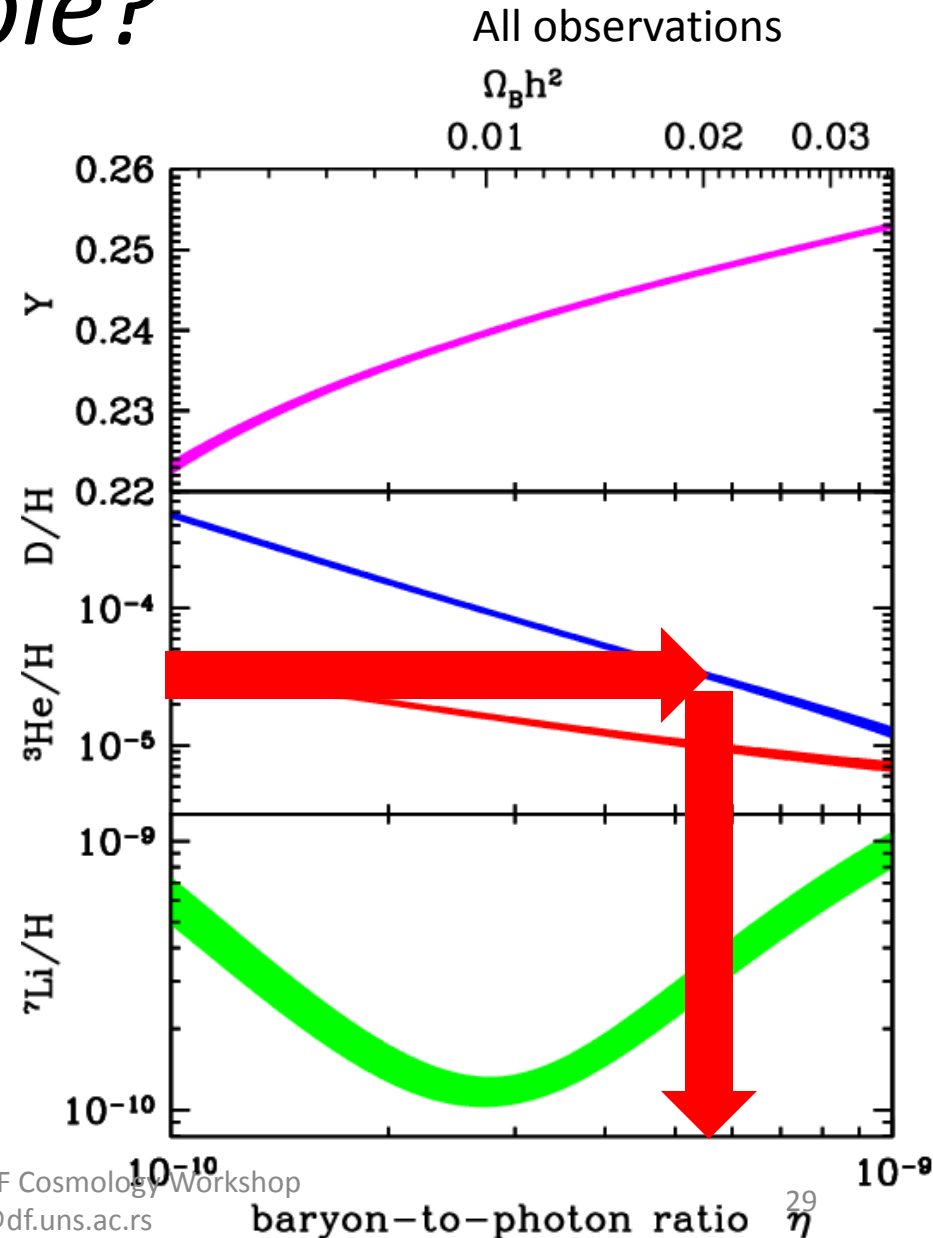
$$Z_{QSO} \sim 0.01 Z_{sol} \Rightarrow D_{QSO} \approx D_p$$

- But scatter!
- Systematics?
- Need more systems!
- SDSS outlook



Simple?

- Have measurements!
- Get baryon density!
- Some uncertainty but consistent
- First indication of dark matter!
 - Deuterium obs. and observed expansion rate not consistent!
 - All matter not baryonic!

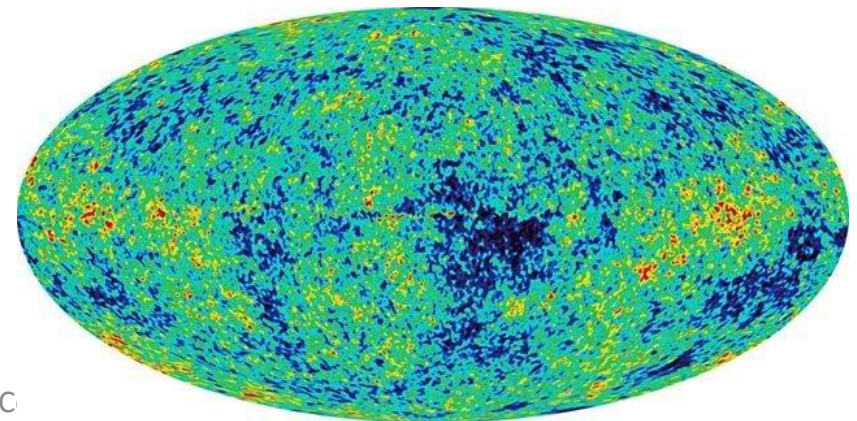


New Light: CMB

- New, independent measurement of baryon density
- WMAP – High-precision cosmology era!
- CMB & BBN – test cosmology!
- WMAP baryon density (Dunkley et al. 2008):

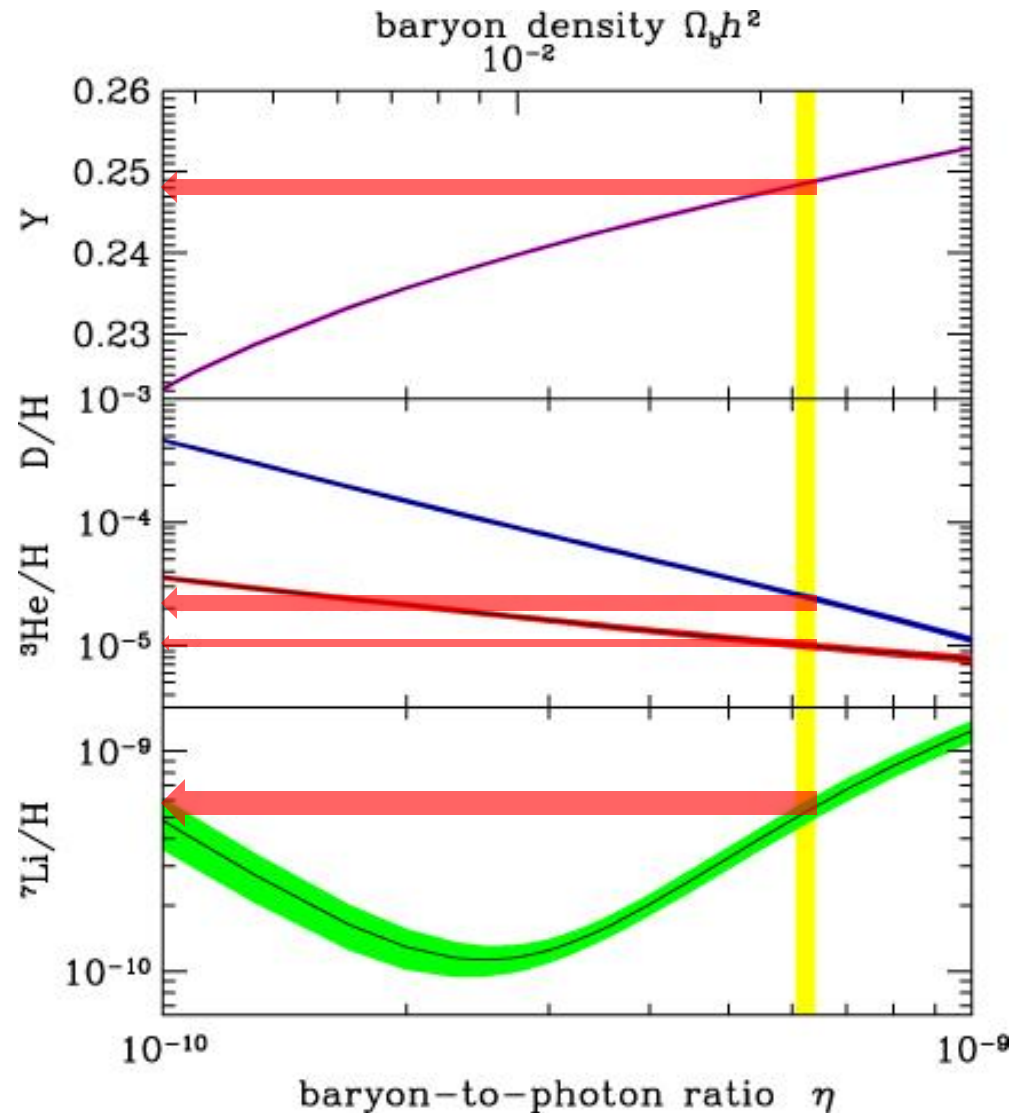
$$\Omega_b h_{100}^2 = 0.02273 \pm 0.00062$$

$$\eta = (6.23 \pm 0.17) \times 10^{-10}$$



BBN & CMB

- WMAP – fix baryon density
- Use BBN to predict primordial abundances
- Easy!
- Compare with observations?

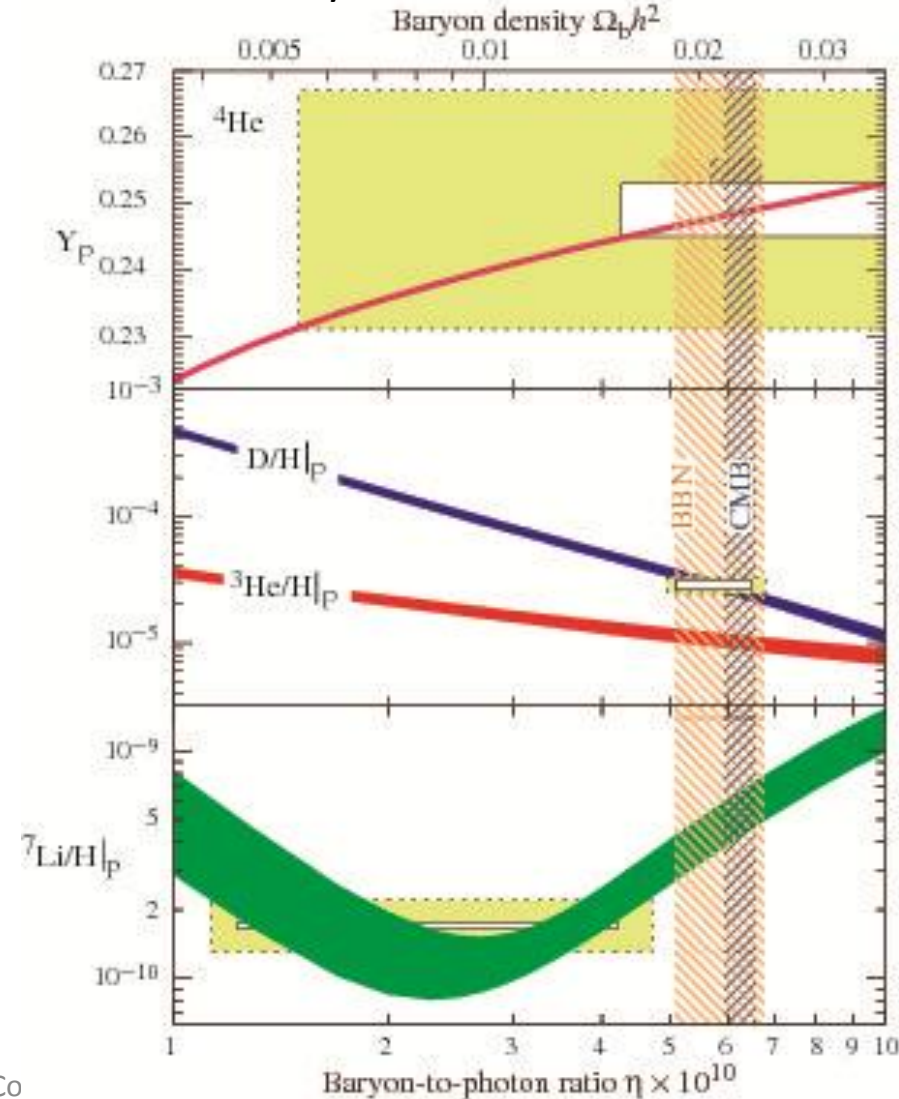


How it all fits?

- BBN theory curves
- CMB – baryon density
- Observation – boxes

- ^4He – OK 😊
- D – right on! 😊
- ^7Li – in trouble! 😞

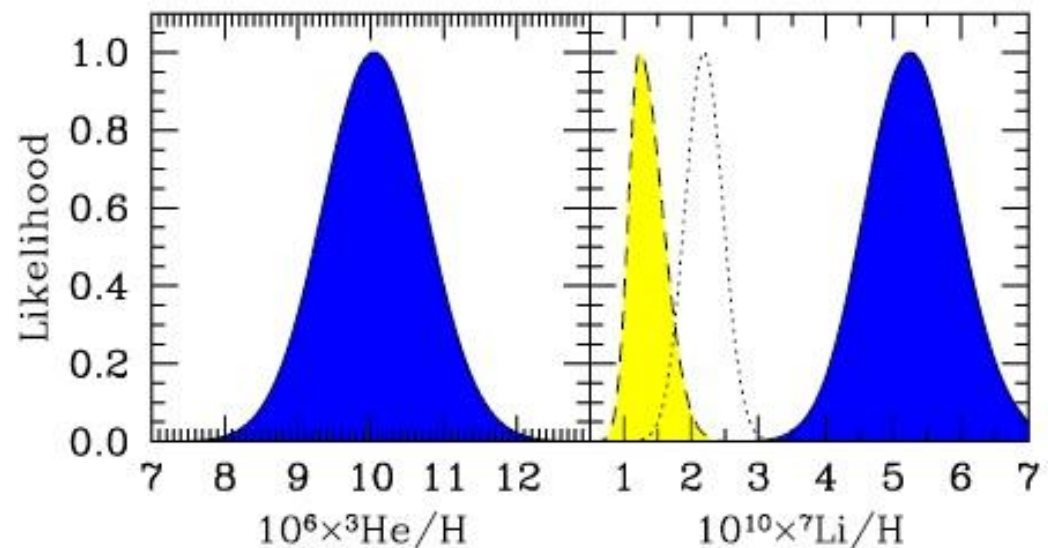
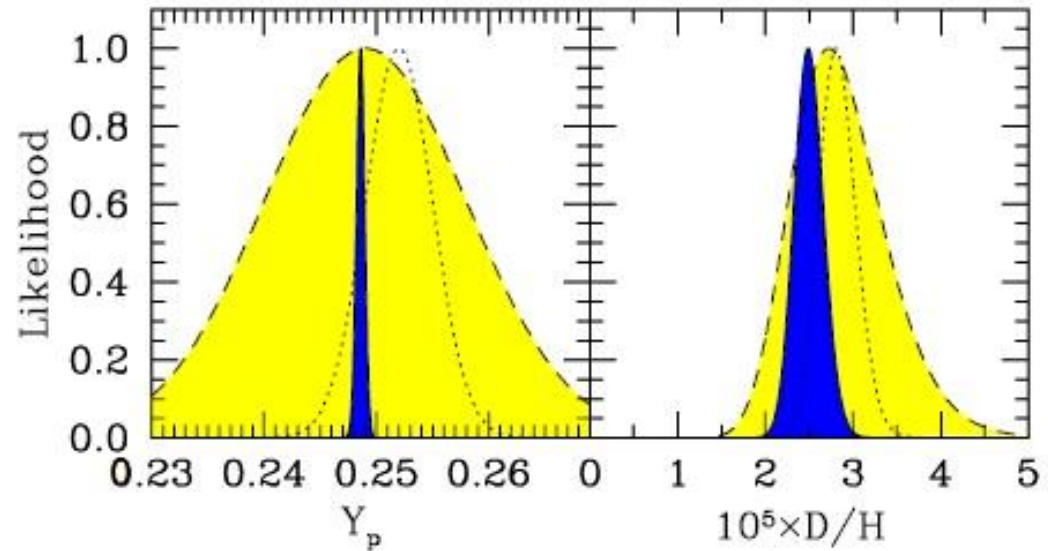
Cyburt et al. 2003, 2008



Concordance?

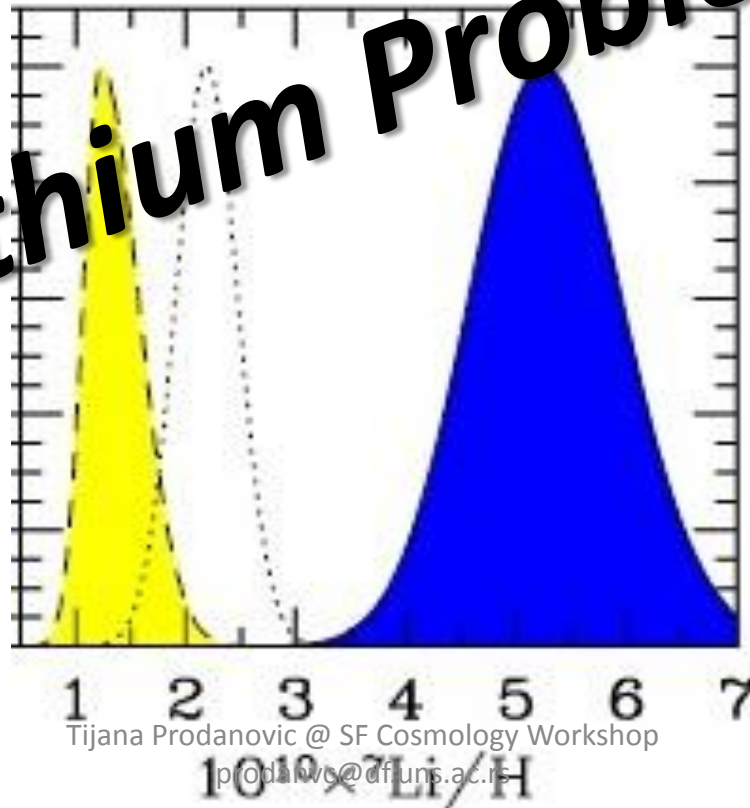
- Cyburt et al. 2008.
- Theoretical (blue)
- Observational (yellow)
- Lithium way off!
Factor of 3-4!

PROBLEM!



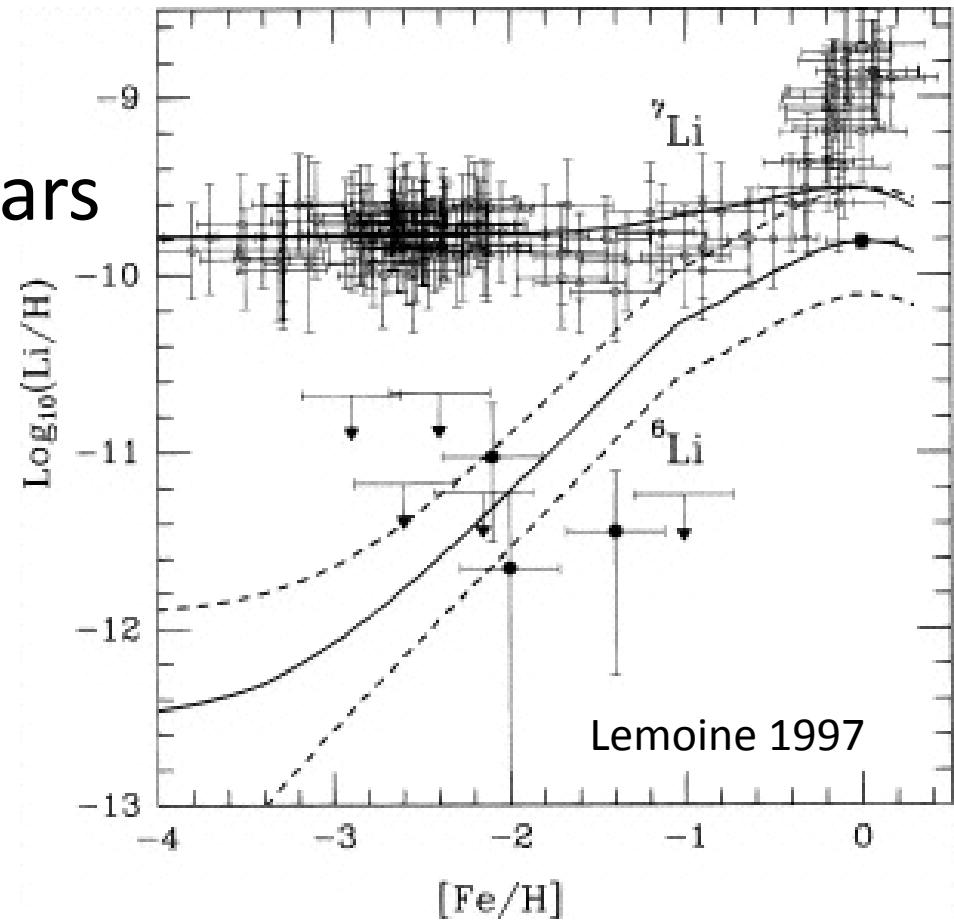


Lithium Problem



Spite Plateau

- Spite & Spite 1982
- Low-metallicity halo stars
- (Close to) Same Li abundance towards lower metallicity
- Very little scatter!
- But different stars
- Primordial plateau?

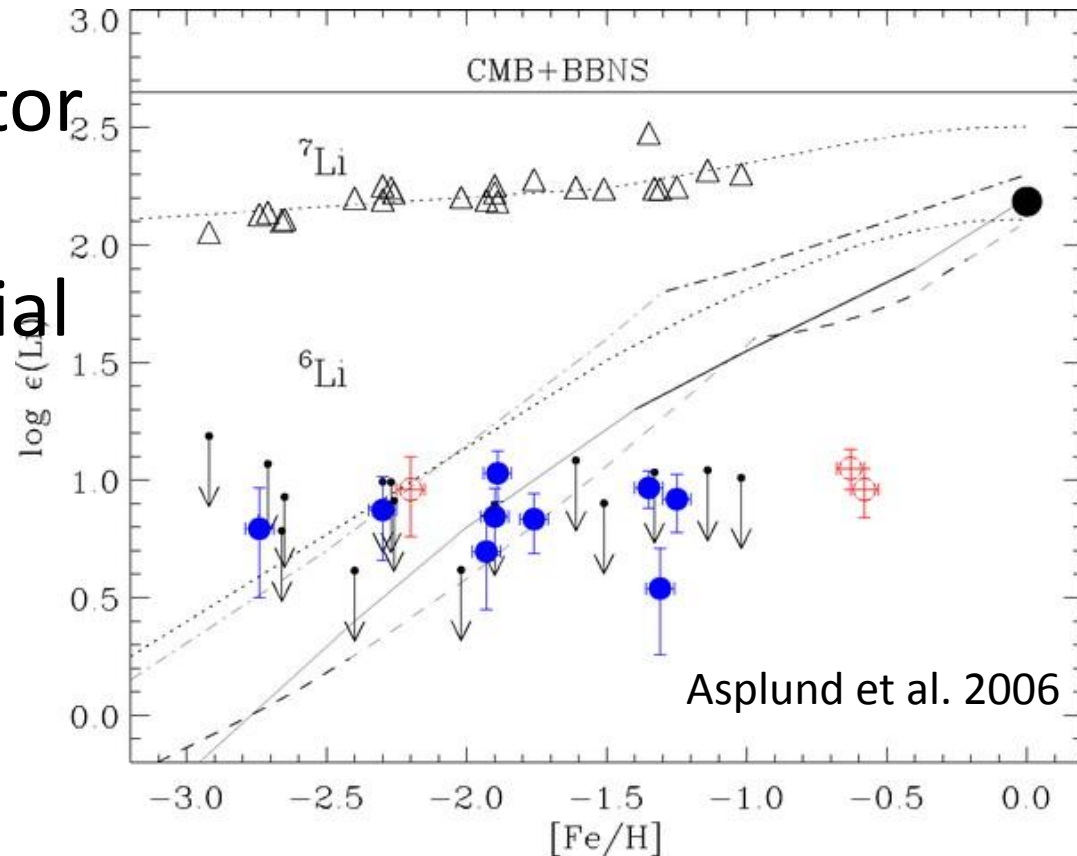


The Lithium Problem

- Spite “plateau” factor of $\sim 2-4$ **lower** than CMB+BBN primordial Li abundance!

$$\left(\frac{{}^7\text{Li}}{H}\right)_p = (5.24^{+0.71}_{-0.62}) \times 10^{-10}$$

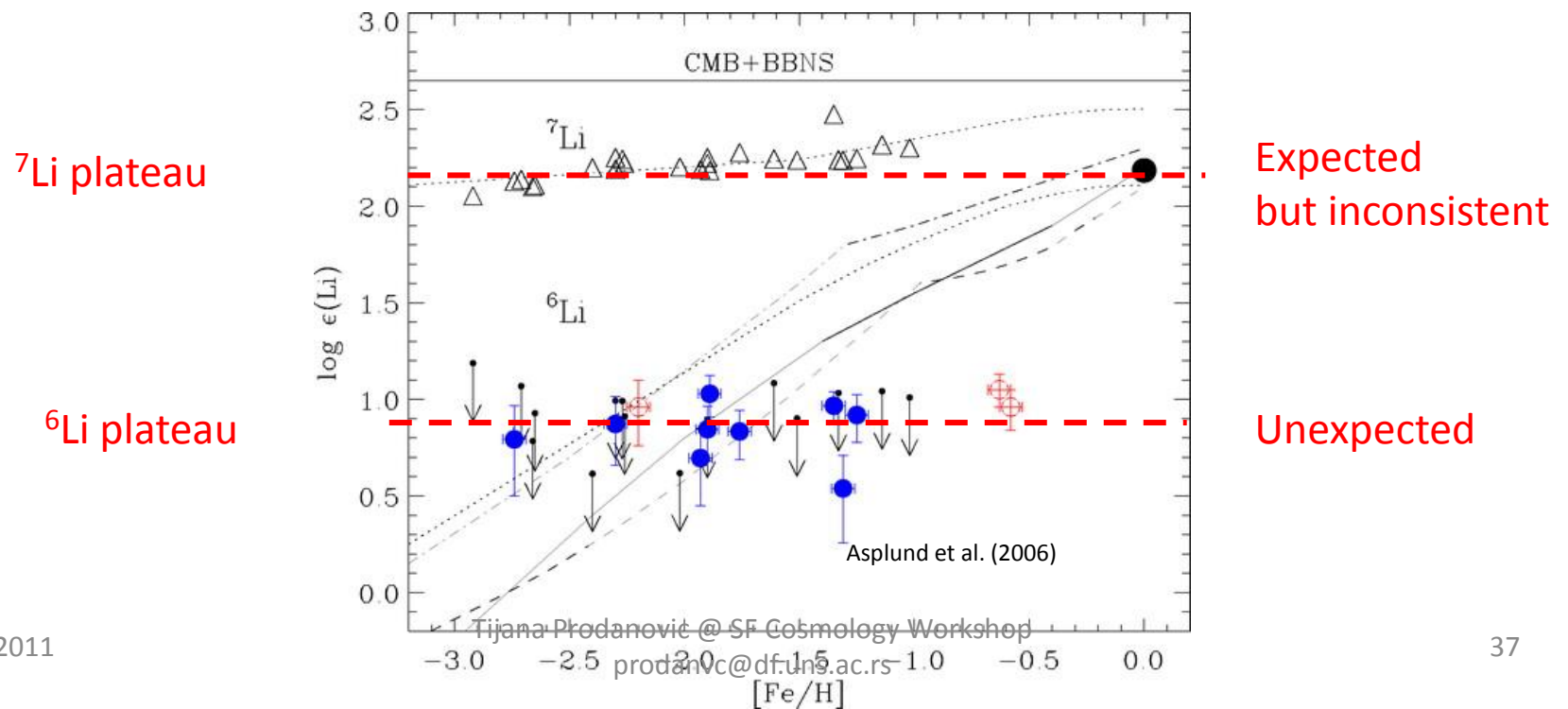
$$\left(\frac{{}^7\text{Li}}{H}\right)_{obs} = (1.23^{+0.68}_{-0.32}) \times 10^{-10}$$



No post-BBN production, but, destruction!?

Lithium Problem Even Worse?

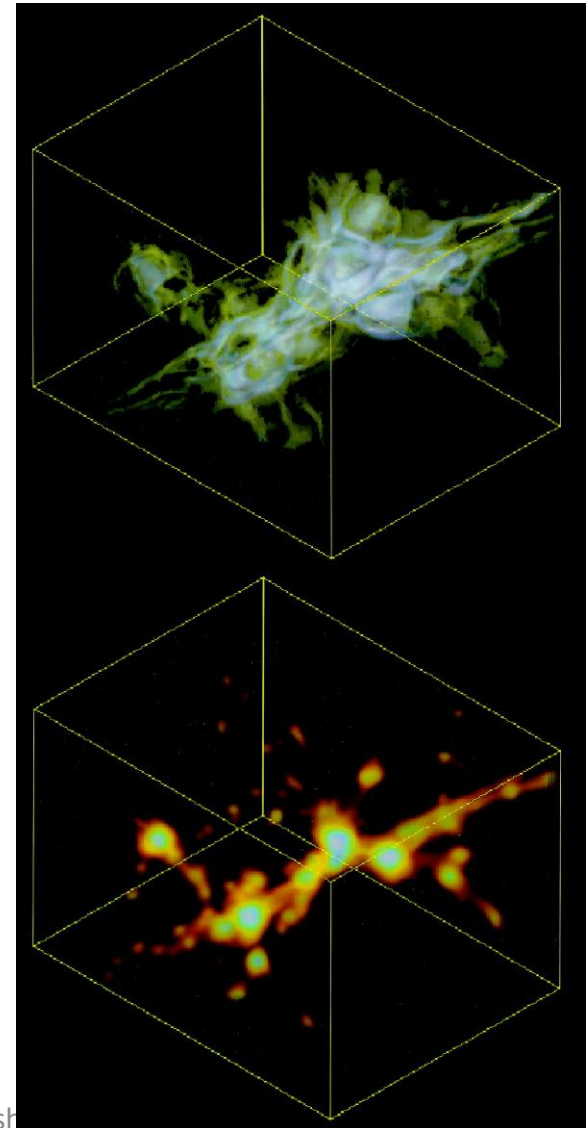
- ${}^6\text{Li}$ “Plateau”? But no BBN source!
- Post-BBN production in cosmic ray interactions
 - Galactic CRs - ${}^6\text{Li}$ increases with metallicity
 - Cosmological CRs? – ${}^6\text{Li}$ constant with metallicity



Lithium Problem Even Worse?

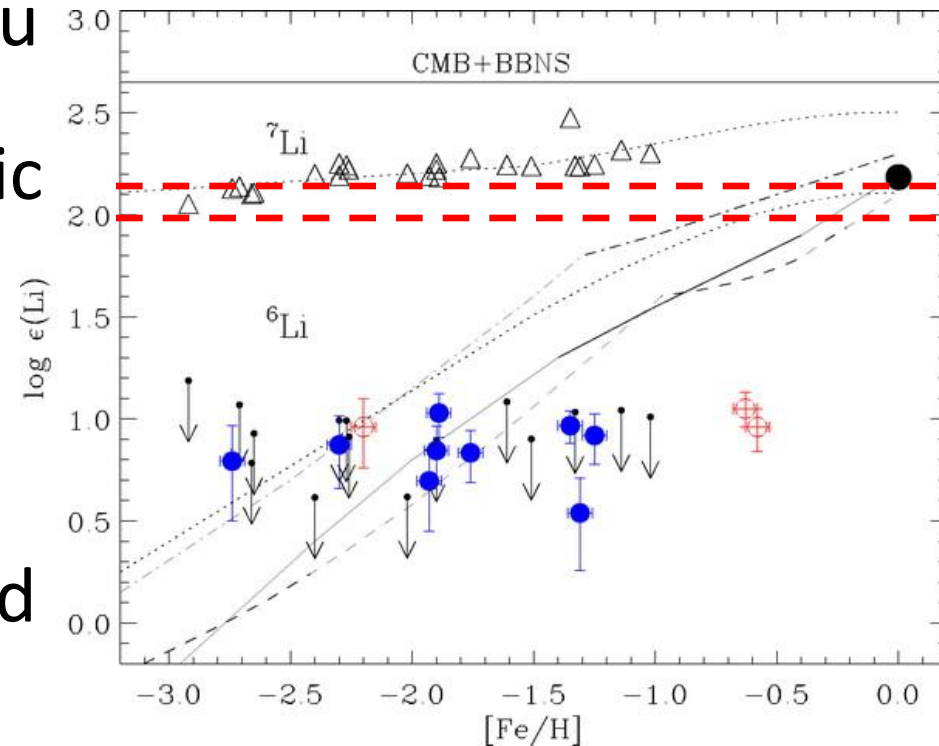
Miniati et al. 2000

- Cosmological cosmic-rays
 - Structure-formation shocks?
Note: Non-detection of gamma-rays by Fermi (Ackermann et al. 2010)
 - Primordial in composition – only H & He
 - Make Li (6,7) without other light elements (Be & B)
 - Would contribute to halo-star Li abundance (Suzuki & Inoue 2002)



Lithium Problem Even Worse?

- Assume entire ${}^6\text{Li}$ plateau made by cosmological/pre-galactic CRs
- Find ${}^7\text{Li}$ made by same CRs
- $\sim 15\%$ of observed Li plateau is pregalactic and not BBN!
- Must correct for it!
- Even larger discrepancy with WMAP+BBN!
- Factor of ~ 5 !



Main Problems

- Abundances below predicted observed over a large metallicity range
- How to destroy Li uniformly?
- Is ${}^6\text{Li}$ plateau real?
- What is pre-galactic source of ${}^{6,7}\text{Li}$?

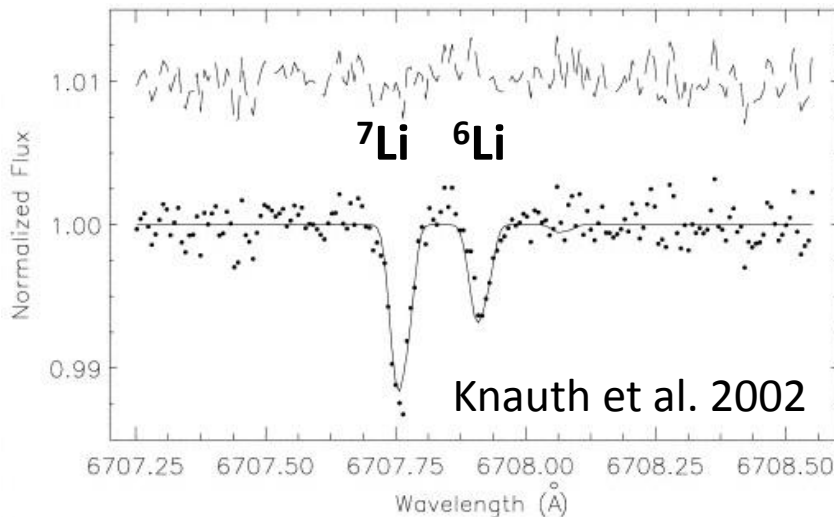
Who is to blame?

- Observations?
- Inferred abundances wrong?
- Problem with stellar atmosphere modeling?
- Theory?
- Inferred abundances correct?
- Find a way to destroy Li before or in stars

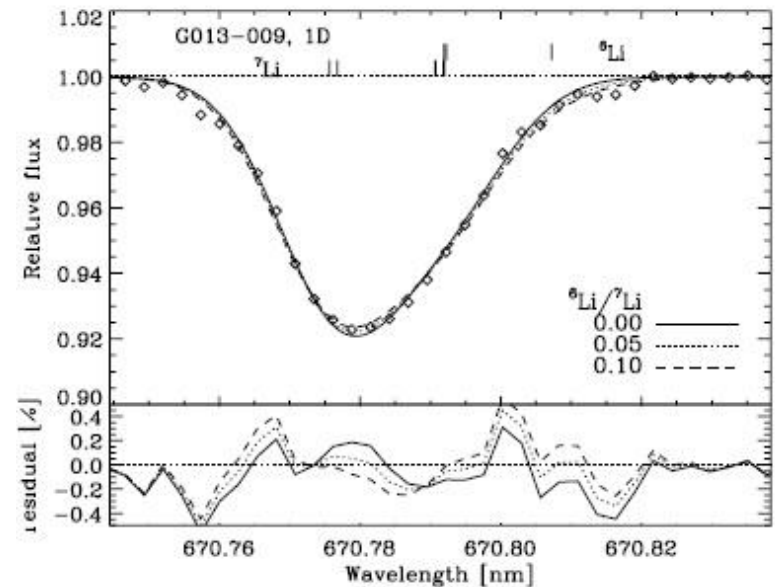


Lithium Observations

- Great in ISM! 😊
 - Both isotopes separated



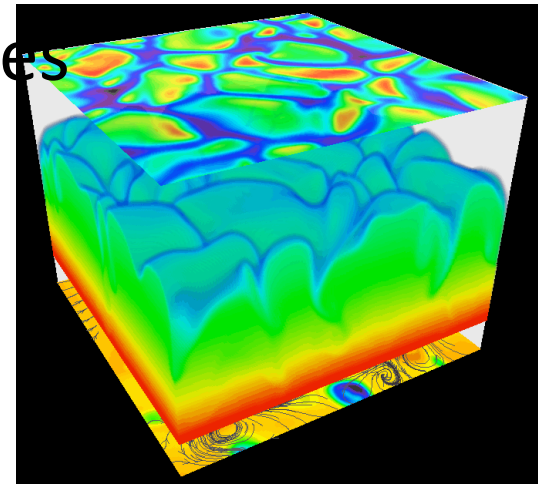
- Messy in stars 😞
 - ${}^6\text{Li}$ just a asymmetry kink on ${}^7\text{Li}$ line – get ratio



Asplund et al. 2006

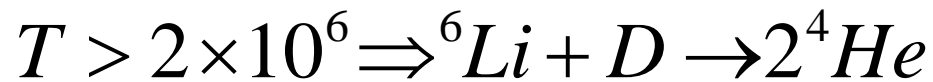
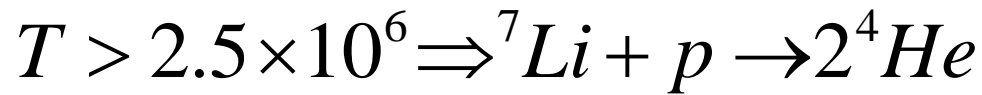
Lithium observations

- Absorption lines in stellar atmospheres
- Modeling! Non-LTE, 1D vs. 3D
 - Li mostly ionized in stellar atmosphere
 - Must get the Li II/Li I ratio
 - Must have correct temperature
- To solve Li problem temperature must be much higher!? $\Delta T \sim 500-600K$?
 - Affects other elements (Be, B, O)
 - Casagrande et al. 2010 – new, detailed estimate of T scale gives $\Delta T \sim 200K$

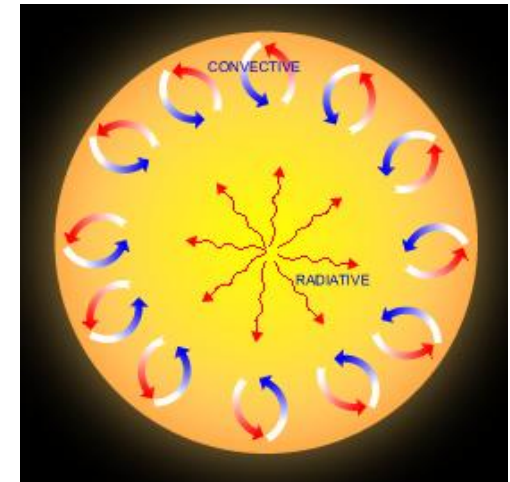


Lithium Theory: Mixing

- Lithium burned easily in stars

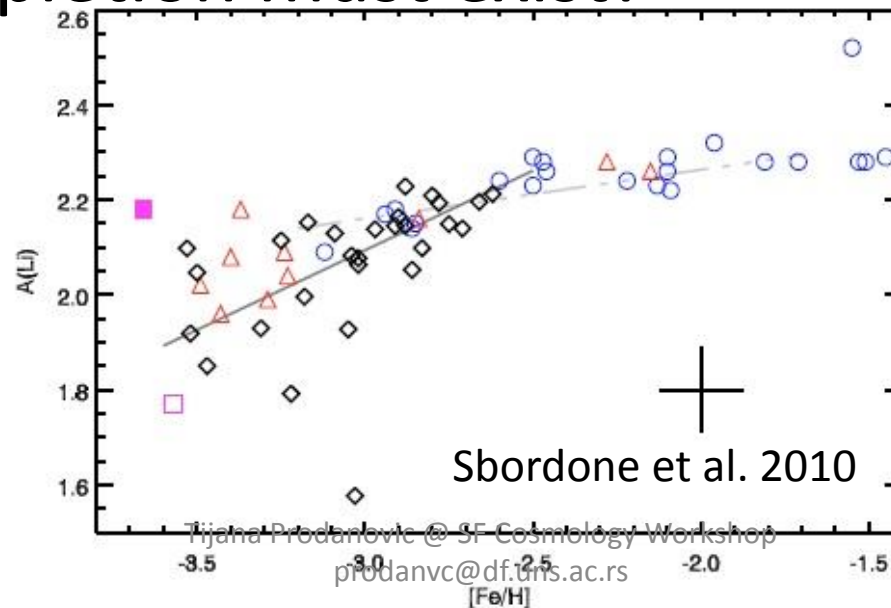


- Destroyed by convection!
 - Surface material mixes in deeper – Li destroyed
 - If destroy ${}^7\text{Li}$ – destroy ${}^6\text{Li}$ even more!
- But – not enough! Not uniform!
 - Different stars – different convective zones?
 - Would cause scatter!
 - Low-metallicity stars have shallower convective zones!



Lithium Depletion

- At very low metallicity $[Fe/H] < -3$
 - Li below Spite plateau
 - Much larger scatter
 - Even more below BBN+WMAP value
- Some depletion must exist!



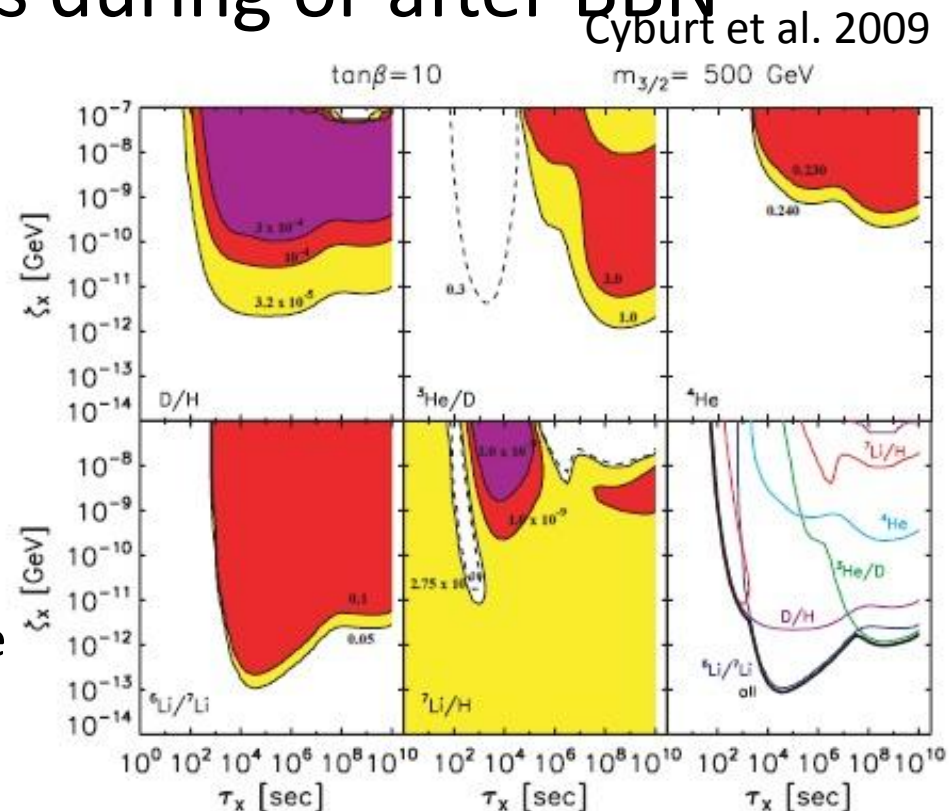
Beyond Astrophysics

- Lithium problem remains
- No conventional solution found...yet
- Must fix ${}^7\text{Li}$ without creating problems with other lite elements!
- Bonus: Same solution a source of ${}^6\text{Li}$?

Beyond Standard Model

- Lightest SUSY partner - Favorite dark matter
- Hadronic decay of longlived parent (next-to-lightest) SUSY particles during or after BBN
- Changes abundances!
- Spallation
- Narrow parameter space that could fix both ${}^6\text{Li}$ and ${}^7\text{Li}$!

White fields – allowed parameter space
Abundance vs. decay time of particle X

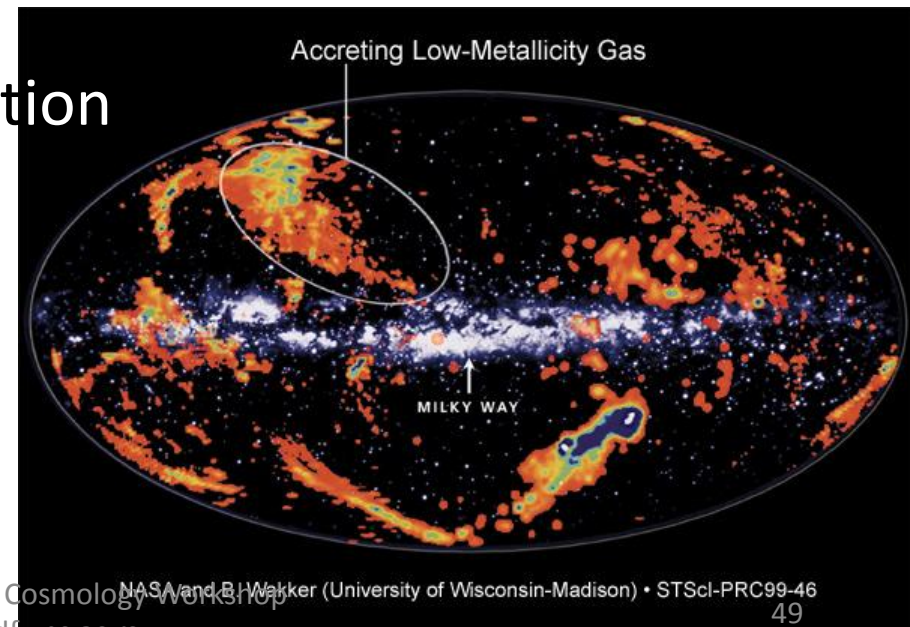


Beyond Standard Model



A Different Approach

- Find another Li site!
- High Velocity Clouds (Wakker & van Woerden 1997)
 - (Some) Low metallicity ($\sim 10\%$ solar)
 - Low dust
 - No stellar modeling
 - Test pre-galactic Li production
- But photoionisation high, column low, measurement difficult



A Different Approach

- Find another Li site!
- Small Magellanic Cloud (Howk et al 2010 proceedings, 2011 submitted)
 - Metallicity ~ 0.25 solar
 - Measure Li abundance (and 7/6 ratio!)
 - Independant probe
 - Stay tuned!



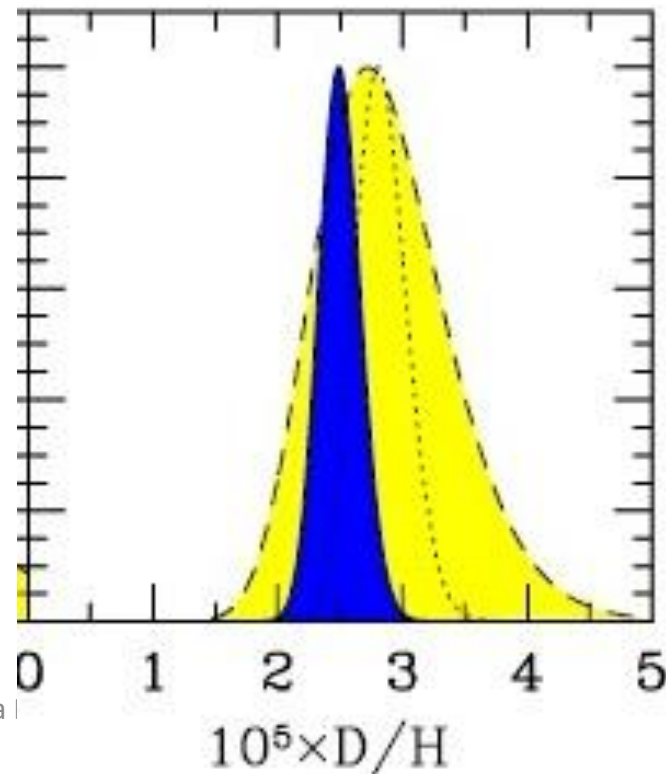
Lithium Problem: Recap

- Factor of ~ 3 discrepancy between BBN+CMB and observed Li abundances in halo stars
- Observational errors – temperature scale?
New destruction channels – mixind, relic particle decay?
- Upcoming tests – LHC, low-metal gas observations
- Solution coming soon! < 10 yr



Deuterium Problem?

- BBN & CMB concordance great!
- Primordial D – cosmology success story
- But locally...



(Local) Deuterium Problem

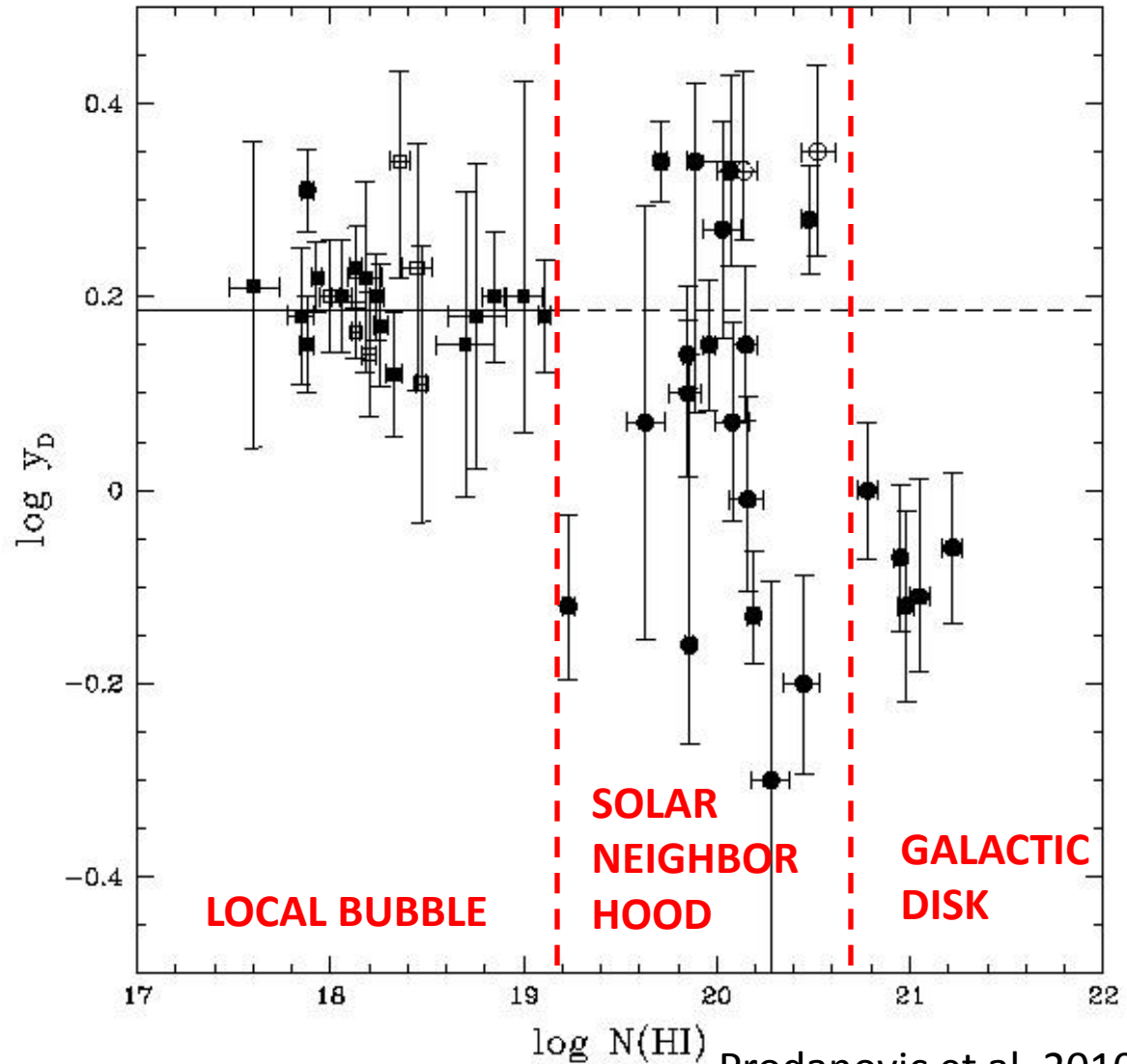
- Simple history
 - Made in BBN $\left(\frac{D}{H}\right)_p \cong 2.82 \times 10^{-5} = 28.2\text{ppm}$
 - Destroyed everywhere – mostly stellar processing
 - Probes gas “virgin” fraction
 - Great for Galactic Chemical Evolution (GCE)
- But large local variations! Factor $\sim 2-3!$
 - Both high (\sim primordial) and low (Linsky et al. 2006)

$$\left(\frac{D}{H}\right)_{ISM} \cong (0.5 - 2.2) \times 10^{-5}$$

Deuterium Variations

Data:
 Linsky et al 2006
 Oliveira & Hebrard 2006

$$y_D \equiv 10^5 \left(\frac{D}{H} \right)$$



Why Care?

- What is the local (ISM) D abundance?
- ISM D very high? (Linsky et al 2006)

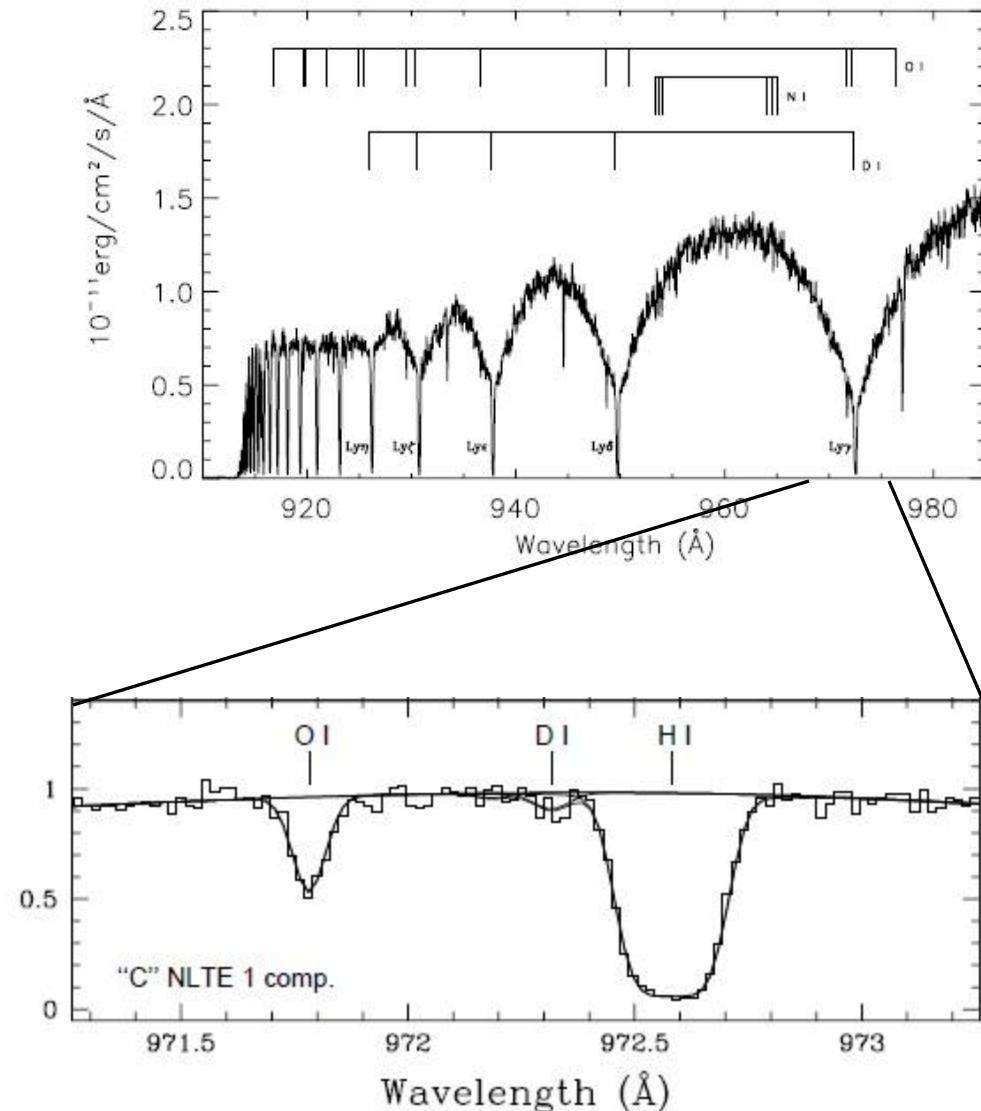
$$\left(\frac{D}{H}\right)_{ISM} \geq (2.31 \pm 0.24) \times 10^{-5}$$

- Implications
 - Very low stellar processing? GCE models disagree
 - Large infall/accretion of primordial material?
 - Higher primordial D abundance?

ISM Deuterium Observations

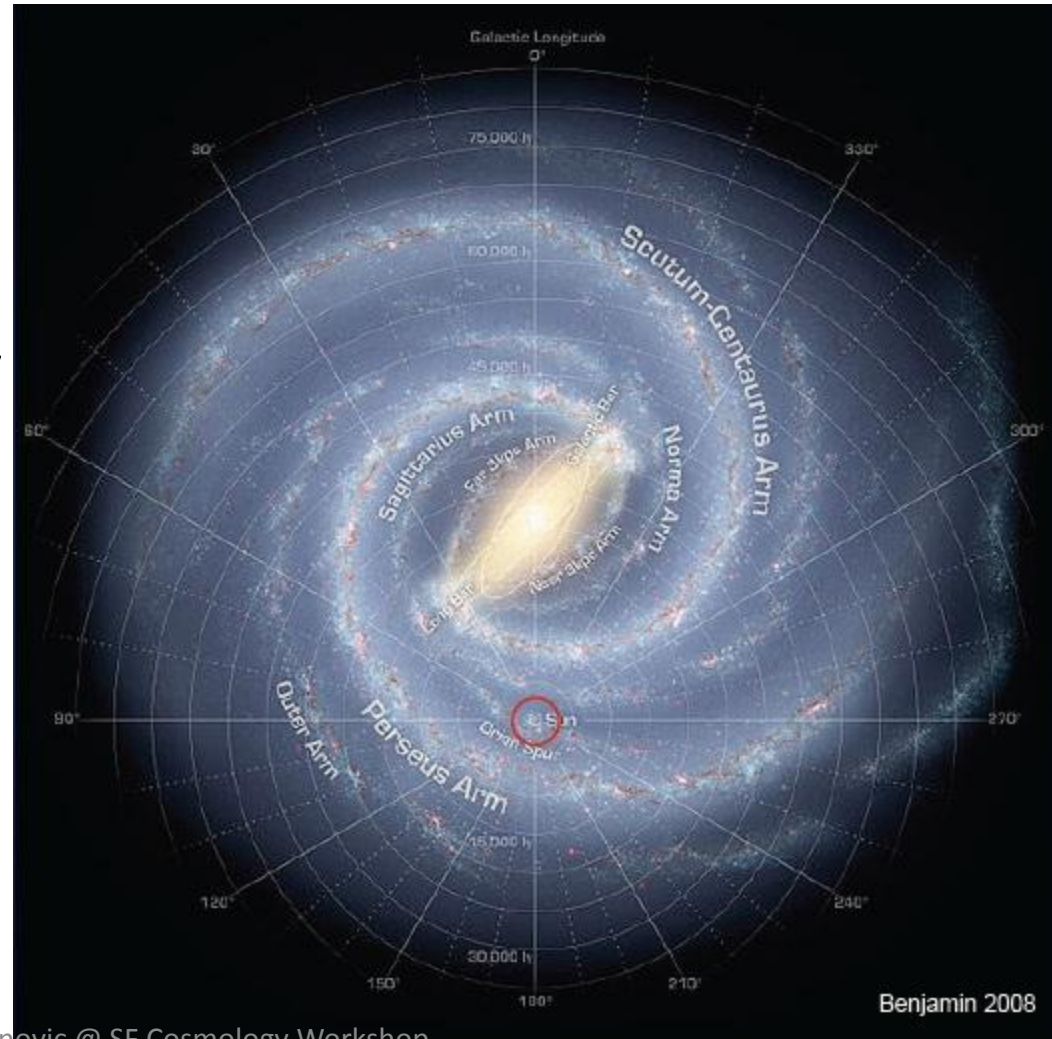
- Neutral interstellar medium
- DI absorption Lyman series in UV stellar spectra
- Most current observations
 - Hubble Space Telescope - ongoing
 - Far Ultraviolet Spectroscopic Explore (FUSE) – not operational

Lemoine et al. 2002



Local Deuterium Observations

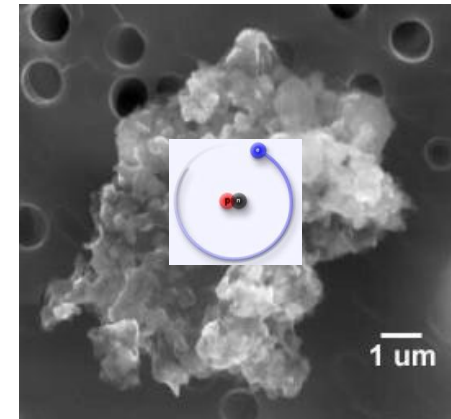
- ISM measurements, but in fact very local
- Only up to ~ 500 pc
- Complicated velocity profiles – superposition of clouds
- Deuterium line “invisible” under H Lyman absorption



Benjamin 2008

Solution?

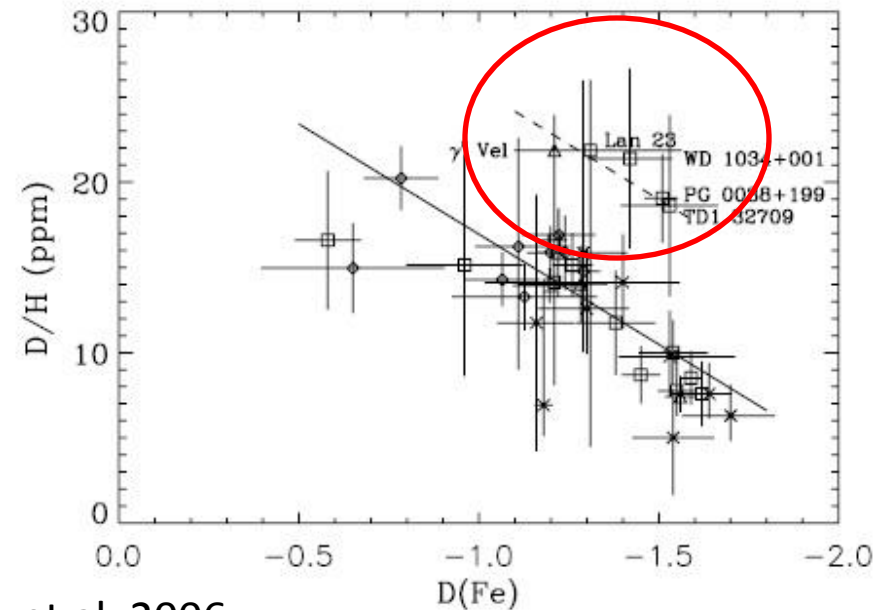
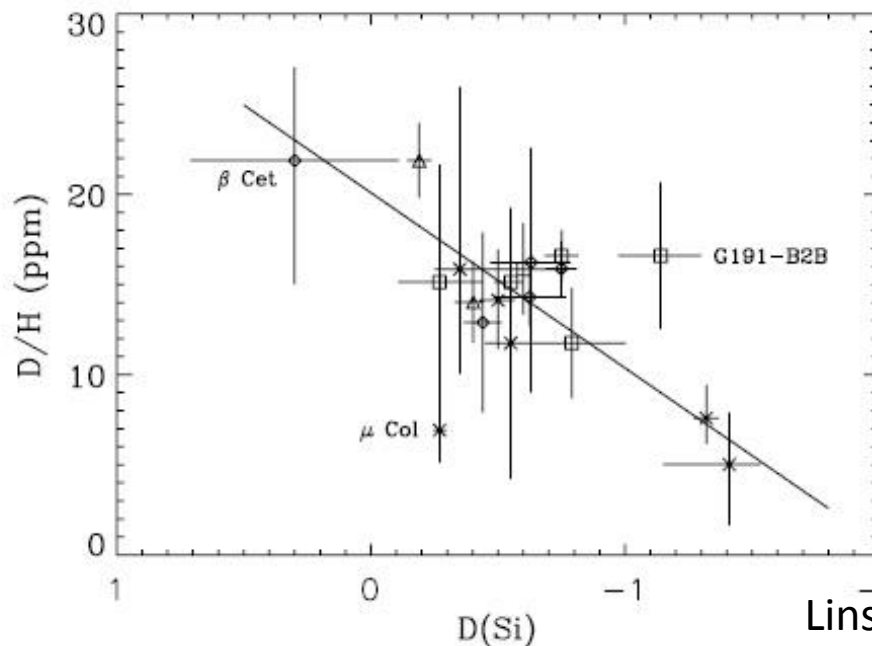
- Deuterium preferentially (compared to H) depleted onto dust! (Jura 1982, Draine 2004, 2006)
- Measure only gas-phase abundance
- Some D fraction locked in dust grains
- Observe – lower bound on “true” abundance
- D should anticorrelate with other refractory elements depletion (Fe, Si, Ti etc.)



Dust Depletion

- D should anticorrelate with other refractory elements depletion (Fe, Si, Ti etc.)

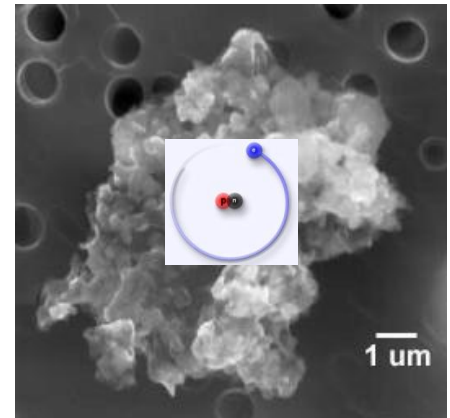
$$D(X) = \log[(X/H)_{\text{gas}} / (X/H)_{\text{sol}}]$$



Linsky et al. 2006

“True” ISM Deuterium?

- Measure lower bound on the “true”, undepleted D
- Highest measured abundance is closest to true value
- Linsky et al. 2006
 - Take 5 highest values
 - “True” ISM D abundance



$$y_{D, ISM+dust} \geq 2.31 \pm 0.24$$

- “True” ISM D = 82% of PRIMORDIAL!

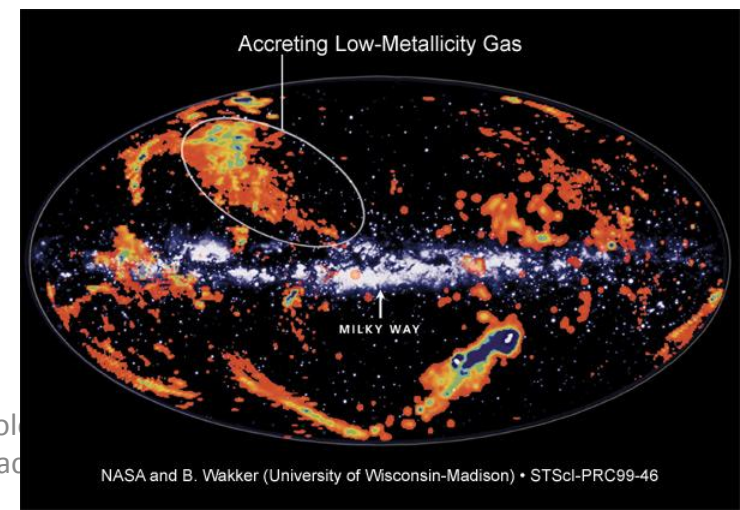
GCE Objects!

- Deuterium destroyed through stellar cycling
- Astration factor (Steigman et al. 2007) $1.4 \leq f_D \equiv y_{Dp} / y_{DISM} \leq 1.8$
- But new *FUSE* high ISM D $f_D \leq 1.22 \pm 0.15$
- Most gas still unprocessed?
- Gas observations say ~20% of present baryonic mass in ISM
- But D observations say ~80% initial gas unprocessed!

Deuterium Facelift?



- High D but normal stellar processing?
- Need infall of (close to) pristine material
 - e.g. High-velocity clouds with low, $\sim 10\%$ solar metallicity
 - Leftover primordial has?
 - Replenish deuterium



Infall Side Effects

- Increase ISM D abundance
- Increase gas content of the Galaxy
- Dilutes metal content of the Galaxy

- **Deuterium and Galactic gas fraction observations powerful constraint of the infall rate**

How much infall?

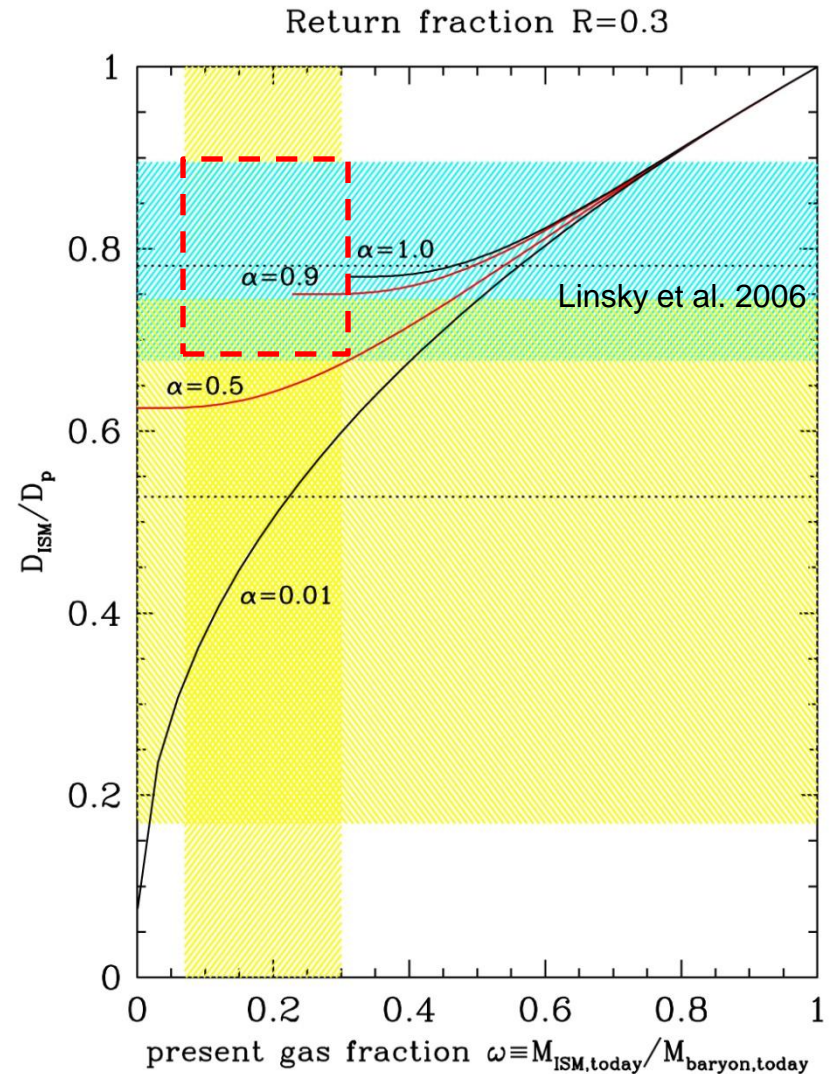
- D vs. gas fraction
- Shaded = observations
- Infall \sim star formation rate

$$\dot{M}_{\text{infall}} = \alpha \psi(t)$$

- Allowed infall rate

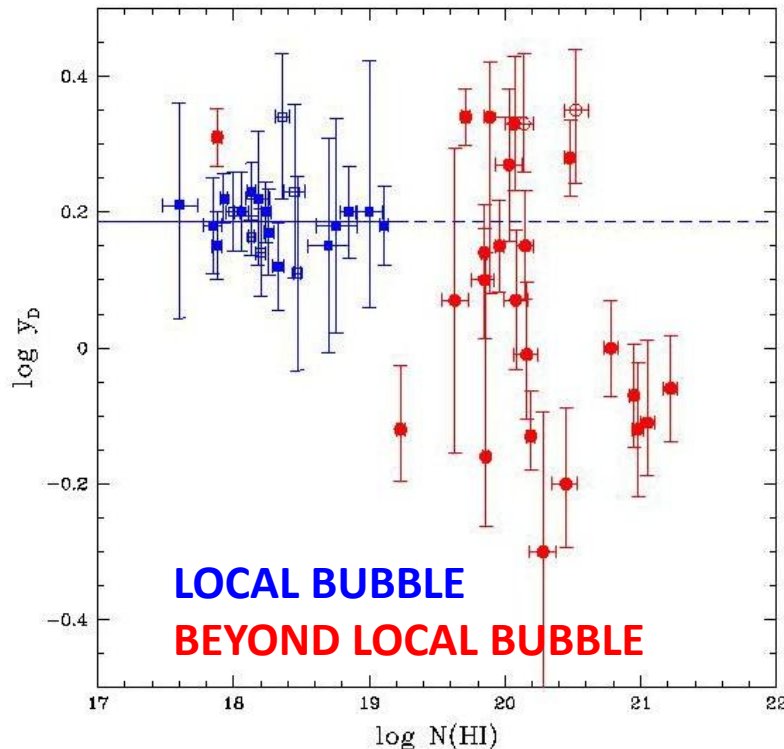
$$0.5 \leq \alpha \leq 1$$

- Almost balances out star-formation!
- Consistent with hierarchical galaxy formation (accretion)
- Still tension with GCE

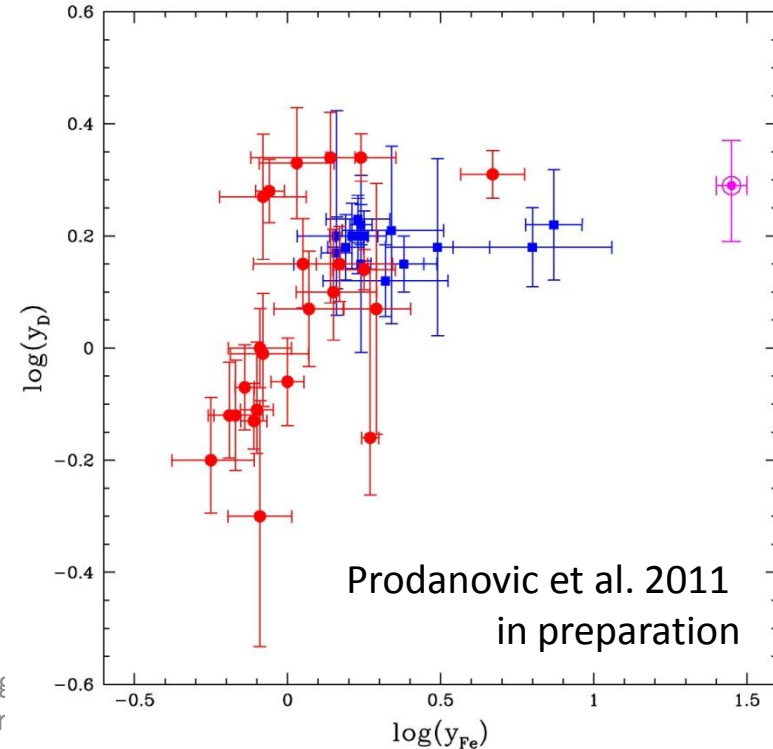


Dust Depletion?

- True at some level, but....
 - Correlation with refractory elements not great
 - D constant in Local Bubble while Fe depleted?



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Prodanovic et al. 2011
in preparation

Dust Depletion?

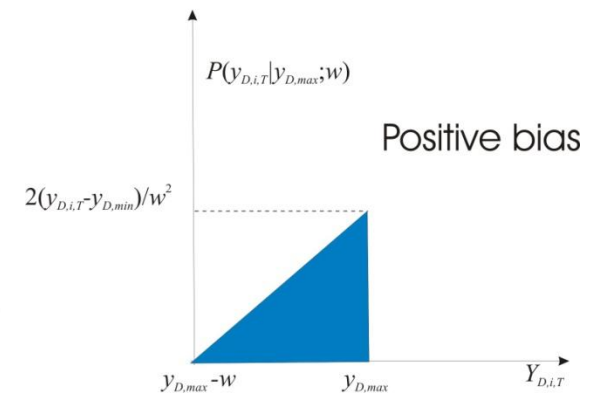
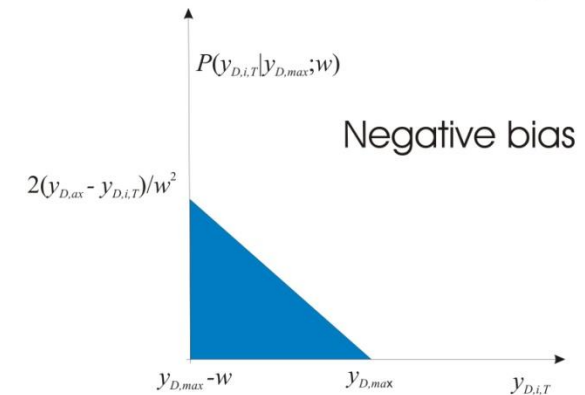
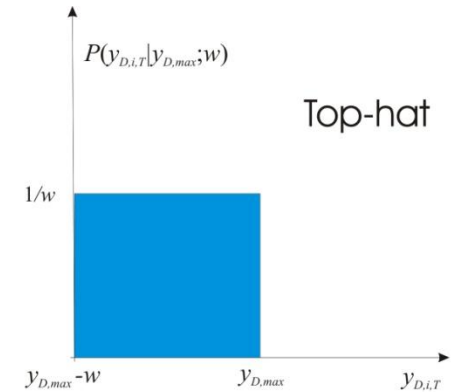
- True at some level, but....
 - Latest “True” ISM D estimate based on 5 highest LOS
 - Might be contaminated by recent infall?
- Need to reevaluate all available data
- Second opinion: A statistical approach

A Statistical Approach

- Hogan et al. (1997) analysis of ^4He data
 - Goal: Find primordial ^4He
 - Have: post-BBN ^4He production contaminated data
 - Assume: There is a post-BBN production
- Take entire deuterium data set – 46 LOS (Linsky et al. 2006)
- Assume nothing about (dust) depletion distribution – only that it exists

Bayesian Maximum Likelihood

- Assume there is depletion
 - Generic depletion probability distribution:
- 1) Top hat – all levels of depletion equally probable
 - 2) Negative bias – favors large depletion
 - 3) Positive bias – favors low depletion



Results: Maximum Likelihood

Prodanovic et al. (2010)

- Top-hat depletion distribution
– highest max. likelihood

- 21 Local Bubble LOS

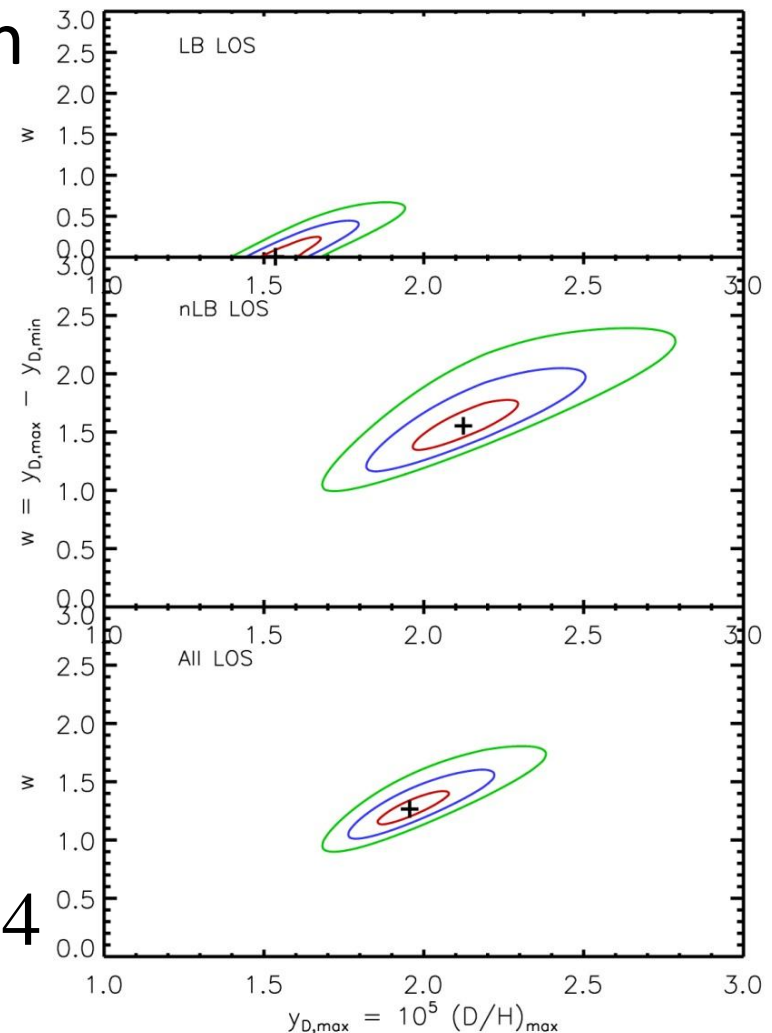
$$y_{D,LB} \cong 1.5 \quad w \cong 0 \quad f_{D,LB} \leq 1.8$$

- 25 non-Local Bubble LOS

$$y_{D,nLB} = 2.1 \quad w = 1.6 \quad f_{D,nLB} \leq 1.3$$

- All 46 LOS

$$y_{D,max} = 2.0 \quad w = 1.3 \quad f_{D,max} \leq 1.4$$



True ISM Deuterium Abundance

- Use all 46 LOS
- Top-hat depletion distribution – highest max likelihood value

$$y_{D,ISM} \geq y_{D,\max} = (2.0 \pm 0.1) \times 10^{-5}$$

- Marginally consistent with Liski et al. (2006)

$$y_{D,ISM+dust} \geq (2.31 \pm 0.24) \times 10^{-5}$$

- Releases tension with GCE models and high-redshift measurements

Problems

- Uniform LB D abundance vs. large scatter in nLB?
 - LB - no depletion? $y_{D,LB} = 1.5$ $w = 0$
 - nLB – large depletion? $y_{D,nLB} = 2.1$ $w = 1.6$
- Is LB uniformly depleted? Why does Fe vary?
- Is nLB enriched with unmixed infall?
- Is Fe really a good depletion indicator for D?
- Do Fe and D deplete on same types of grains?
- Dust grain physics still unknown territory...

Primordial Element Problem(s)

- Lithium is still a problem
 - Probably too large discrepancy to be observational
 - Need some way to destroy
 - In stars – deeper mixing?
 - Decay of recil particles at BBN epoch – LHC?
 - Need new site! SMC measurements soon!
- Deuterium – BBN + WMAP concordance
 - OK at high- z but locally a pressing problem
 - Can have important cosmological consequences
 - No need to panic...yet



Thank You!



How much infall needed?

- Build a “keep it simple” model

- Infall and NO outflow

- Infall rate proportional to star-formation rate $\psi(t)$

$$\dot{M}_{\text{infall}} = \alpha \psi(t)$$

- Define gas mass fraction

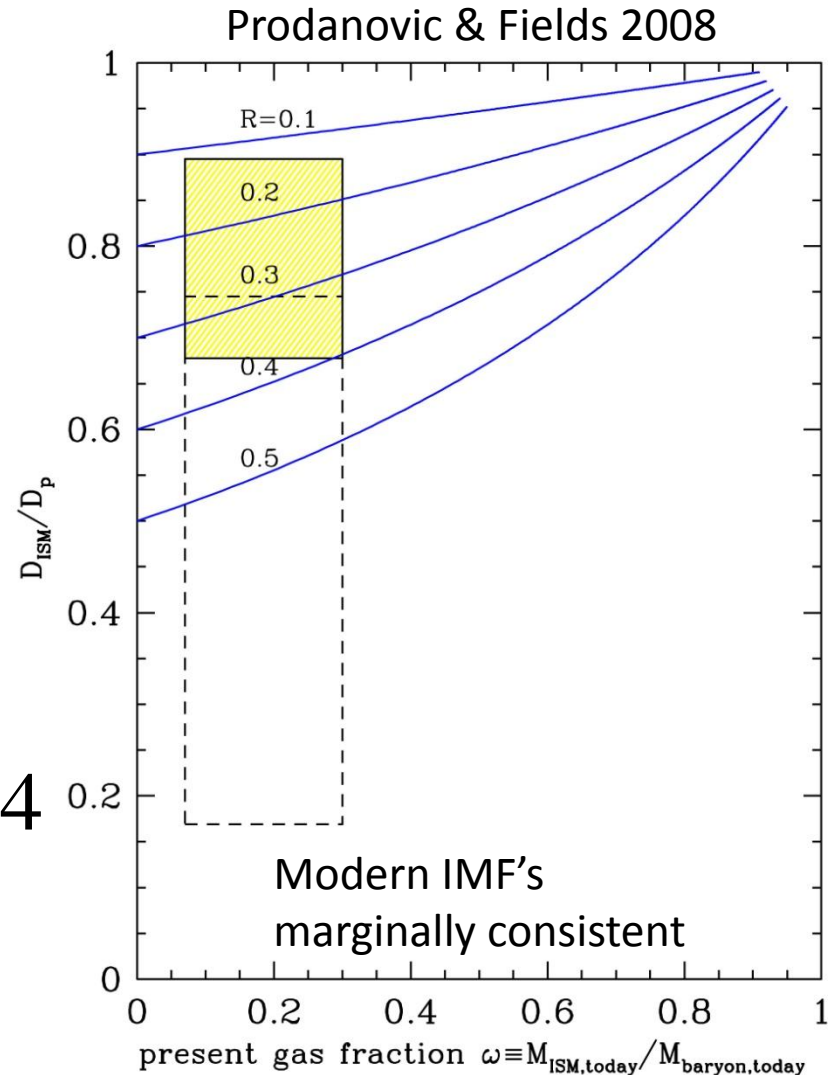
$$\omega(t) \equiv M_{\text{ISM}}(t) / M_{\text{baryon}}(t)$$

- Specify return fraction R – fraction of initial stellar mass that is returned to ISM (follows from Initial mass function); e.g. $R = 0.3$ from Salpeter IMF

IMF Constraints

- At late times D and gas fraction approach minimum values
- Limiting curves above which no solutions for range of return fractions
- Allowed only $0.1 < R \leq 0.4$
- Modern IMFs demand

$$R = 0.4$$



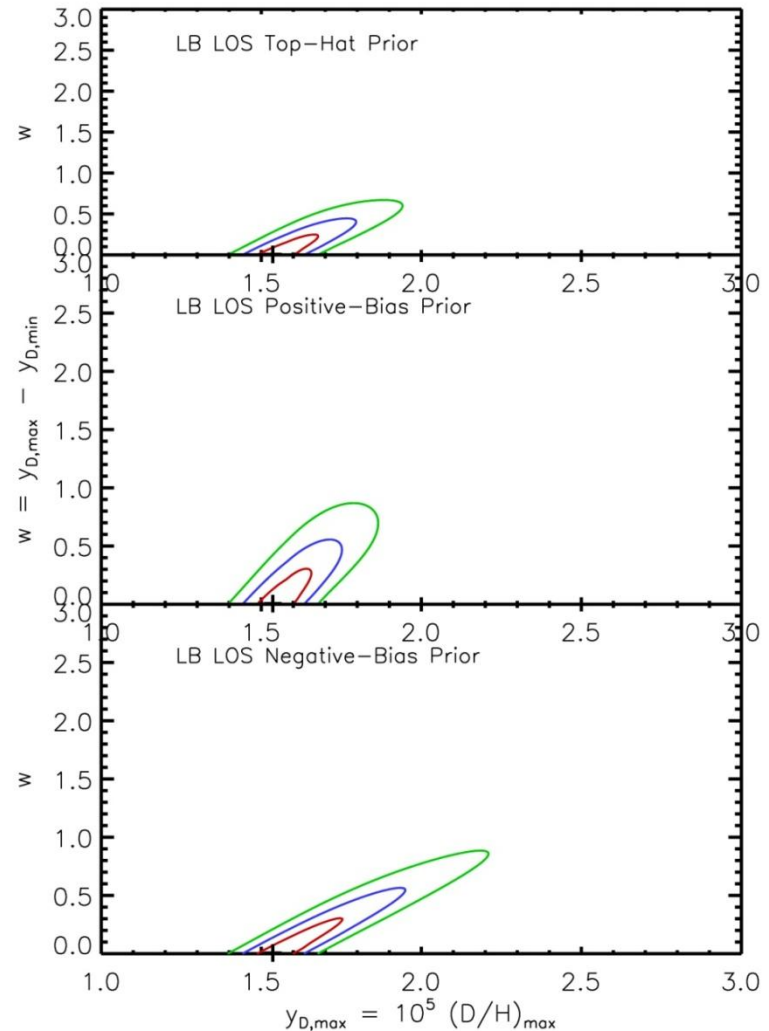
Results: Local bubble

- 21 Local Bubble LOS
- 1,2,3 σ contours
- All depletion distributions yield

$$y_{D,LB} \cong 1.5 \quad w \cong 0 \quad f_{D,LB} \leq 1.8$$

- Local Bubble
 - Consistent with no depletion
 - Consistent with GCE

Prodanovic, Steigman & Fields (2009)
arXiv:0910.4961



D vs. Metal yields

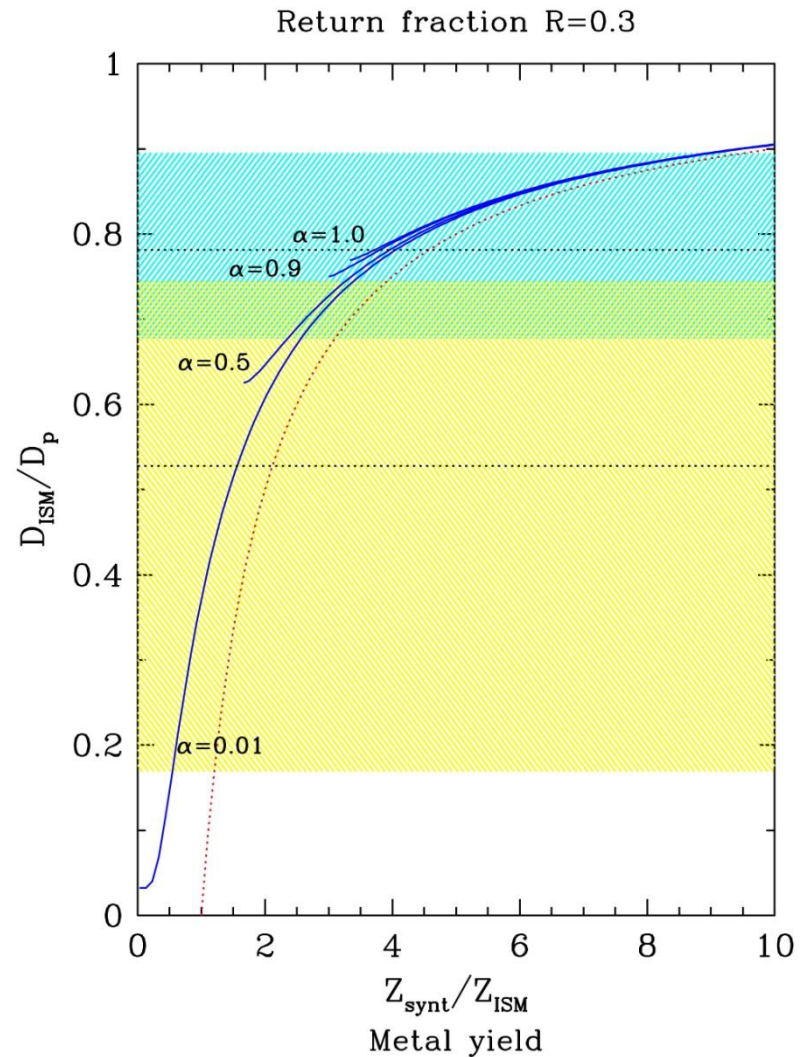
Freshly synthesized metals Z_{synt}

SN metal yield $Z_{SN} \sim 10Z_{sol}$

Present reasonable estimates

$$Z_{synt} / Z_{ISM} \approx 4$$

consistent with large or no infall
since all curves converge.



Model: details

$$\frac{dM_{ISM}}{dt} = -(1-R)\psi + \alpha\psi$$

$$\frac{d}{dt}(DM_{ISM}) = -D\psi + D_p\alpha\psi$$

Where D is the deuterium mass fraction defined as:

$$D \equiv X_D \equiv \frac{\rho_D}{\rho_{baryon}} \cong 2 \left(\frac{D}{H} \right) X_H$$

Taking $\mu \equiv M_{ISM}(t)/M_{baryon}(t=0)$ we get:

$$\frac{D(t)}{D_p} = \frac{R}{\alpha + R} \left(\frac{\alpha}{R} + \mu^{\frac{\alpha+R}{1-\alpha-R}} \right)$$

which we can express in terms of the present gas mass fraction by using:

$$\omega(t) \equiv \frac{M_{ISM}}{M_{baryon}} = \frac{1-R-\alpha}{1-R-\alpha\mu(t)} \mu(t)$$

model: details – Return fraction

Approximate: $m_{ej}(m) = m - m_{rem}(m)$

Then, define return fraction for each progenitor mass as: $R(m) \equiv m_{ej} / m$

To find a global return fraction must specify the IMF: $\phi(m) \equiv dN / dm$

$$R = \frac{\int_{m_L}^{m_U} dm \cdot R(m) \cdot m \cdot \phi(m)}{\int_{m_L}^{m_U} dm \cdot m \cdot \phi(m)}$$

For mass ranges $8 \leq m_{SN} / M_{sol} \leq 100$ and $0.8 \leq m_{AGB} / M_{sol} \leq 8$

and Salpeter IMF $\phi(m) \propto m^{-2.35}$

we find return fraction $R = 0.31$

Modern IMFs are flatter in the high-mass regime \rightarrow more high-mass stars \rightarrow more ejecta
 \rightarrow larger return fractions $R \sim 0.4$

model: details - envelope

$$\frac{D(t)}{D_p} = \frac{R}{\alpha + R} \left(\frac{\alpha}{R} + \mu^{\frac{\alpha+R}{1-\alpha-R}} \right)$$

$$\omega(t) \equiv \frac{M_{ISM}}{M_{baryon}} = \frac{1-R-\alpha}{1-R-\alpha\mu(t)} \mu(t)$$

For large infall where $R + \alpha \geq 1$

$$\left. \frac{\alpha + R}{1 - \alpha - R} < 0 \right\} \Rightarrow \mu^{\frac{\alpha+R}{1-\alpha-R}} \rightarrow 0$$

$$1 - R \ll \alpha\mu(t) \Rightarrow$$

$$\frac{1 - R - \alpha}{1 - R - \alpha\mu(t)} \mu(t) \rightarrow \frac{1 - R - \alpha}{-\alpha\mu(t)} \mu(t)$$

$$\frac{D_{\min}}{D_p} \rightarrow \frac{\alpha}{\alpha + r}$$

$$\omega_{\min} \rightarrow 1 - \frac{1 - R}{\alpha}$$

For small infall where $R + \alpha < 1$

$$\mu \rightarrow 0 \Rightarrow \left\{ \begin{array}{l} \mu^{\frac{\alpha+R}{1-\alpha-R}} \rightarrow 0 \Rightarrow \frac{D_{\min}}{D_p} \rightarrow \frac{\alpha}{\alpha + R} \\ \omega_{\min} \rightarrow 0 \end{array} \right.$$

A *BAYESIAN* approach

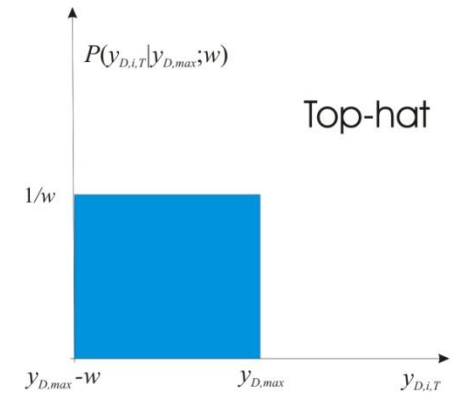
- Finding maximum likelihood $\{y_{D,\max}, w\}$

$$L(y_{D,\max}, w) = \prod_i \int dy_{D,i,T} P(y_{D,i} | y_{D,i,T}) P(y_{D,i,T} | y_{D,\max}; w)$$

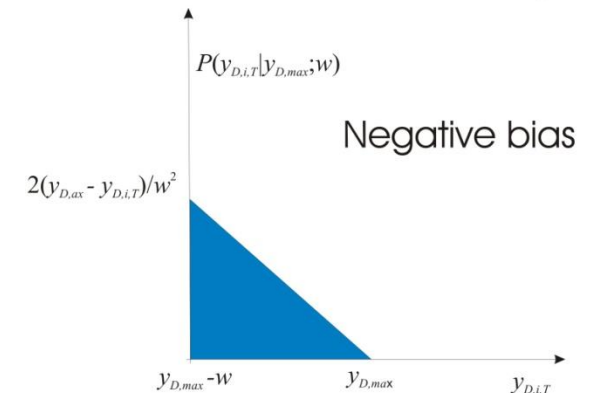
- $P(y_{D,i} | y_{D,i,T})$ - Probability distribution
 - Relates what is measured to what should be measured (true) if it were no errors
 - Assume Gaussian
- $P(y_{D,i,T} | y_{D,\max}; w)$ - **Depletion probability distribution**
 - Probability of finding the true, dust depleted ISM D given $y_{D,i,T}$ the max. gas phase D $y_{D,\max}$ and depletion w

Choice: Depletion distributions

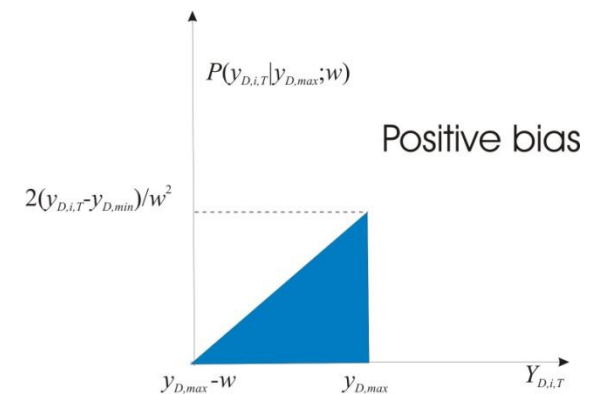
1) Top hat – all levels of depletion equally probable



1) Negative bias – favors large depletion



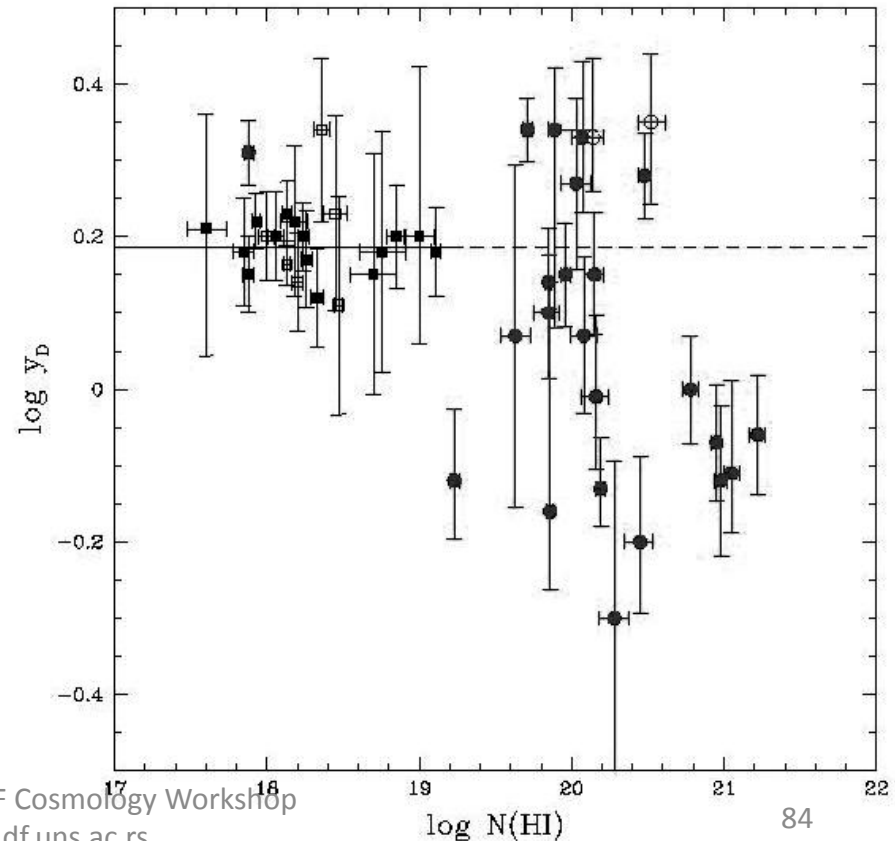
1) Positive bias – favors low depletion



LB vs. Non-LB

- Local Bubble very different from non-Local Bubble
- LB – blue
 - Uniform
- nLB – red
 - Large scatter
- First treat separately

Prodanovic, Steigman & Fields (2009)
arXiv:0910.4961



Results: Depletion Distributions

Prodanovic et al. (2010)

- All 46 LOS
- Different depletion distribution comparison

– Top-hat

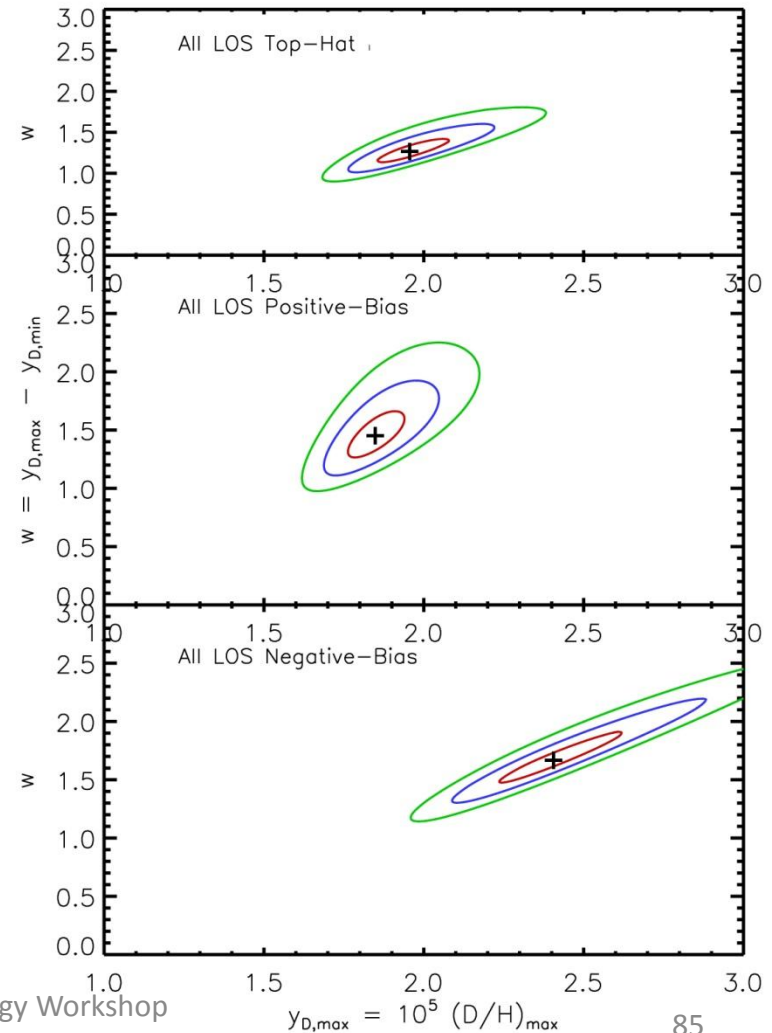
$$y_{D,nLB} = 2.0 \quad w = 1.3$$

– Positive-bias

$$y_{D,nLB} = 1.8 \quad w = 1.5$$

– Negative-bias

$$y_{D,nLB} = 2.4 \quad w = 1.7$$



Abundances 101

- Log abundances

$$\log y_i \equiv \log \varepsilon_i = \log \frac{i}{H} + 12$$

$$\log \varepsilon_H = 12$$

Eg. $\log \varepsilon_{Li} = 2 \Rightarrow \frac{Li}{H} = y_{Li} = 10^{-10}$

- Elemental ratios relative to Solar

$$\left[\frac{A}{B} \right] = \log \left(\frac{n_A}{n_B} \right) - \log \left(\frac{n_A}{n_B} \right)_{sol}$$

eg. metallicity $\left[\frac{Fe}{H} \right] = -1.0 \Rightarrow y_{Fe} = 3.2 \times 10^{-6}$

Abundances 101

- Ratio of some element to another (usually H)
- Notations/Representations

– Mass fraction $X_i = \frac{\rho_i}{\rho_{tot}}$

$$X \equiv X_H \quad Y \equiv X_{He} \quad Z \equiv X_{metal}$$

$$X + Y + Z = 1$$

Solar values $0.70 + 0.28 + 0.02 = 1$

– Abundance (wrt H, by number) $\frac{i}{H} \equiv y_i \equiv \frac{n_i}{n_H}$

$$y_{He,sol} = 0.1 \quad y_{Fe,sol} \equiv \left(\frac{Fe}{H} \right)_{sol} = 3.2 \times 10^{-5}$$